

Presentation 33

Pugh: Using GeoGebra to Model Four Representations of Linear Equations

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“And I’m calling on our nation’s governors and state education chiefs to develop standards and assessments that don’t simply measure whether students can fill in a bubble on a test, but whether they possess 21st Century skills like problem solving and critical thinking and entrepreneurship and creativity.”

President Obama, 1 March 2009

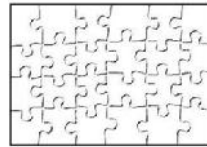
Using GeoGebra to Model Four Representations of Linear Equations

David Pugh, EdD & much material from Dr. Alan Schoenfeld, UC Berkeley
dapugh@rochester.k12.mn.us

Typical Student Beliefs

Schoenfeld

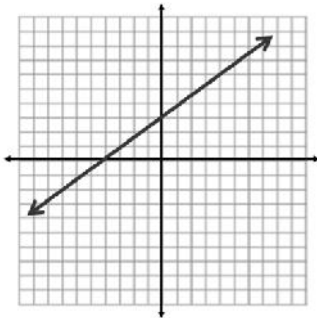
- Students who have understood the mathematics they have studied will be able to solve any assigned problem in five minutes or less.



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My “Principal” Lesson



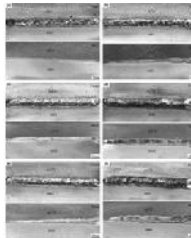
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Typical Student Beliefs

Schoenfeld

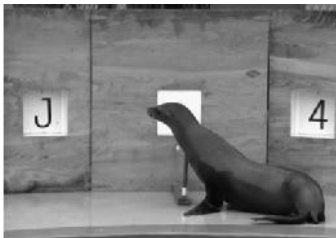
- The mathematics learned in school has little or nothing to do with the real world.



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Are You Smarter Than a Sea Lion?



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Typical Student Beliefs

Schoenfeld

- Ordinary students cannot expect to understand mathematics; they expect simply to memorize steps and apply them to a problem.

- Go to Broadway
- South 3 blocks
- Turn Right
- West 1 block
- On your left.



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The bottom line

Doyle, W. (1988). Work in mathematics classes: The context of students' thinking during instruction. *Educational Psychologist*, 23(2), 167-180.

Although students often accomplish a large amount of work, they seldom appear to be faced with tasks in which they are required to struggle with meaning. Of course, they often struggle with the meaning of work: What are they supposed to do, when do they have to finish, what is the answer to the fifth problem? But, meaning itself is seldom at the heart of the work they accomplish.

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Using GeoGebra

The screenshot shows the GeoGebra interface with a coordinate plane on the left and a 'Description' panel on the right. The description panel contains the text: 'We collect 5 ounces of honey for every 7 bees.' Below this, there is a table with columns 'x' and 'y', and a 'Rate of Change' section showing the formula $\Delta y = \frac{\Delta y}{\Delta x}$.

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What is Math?

Schoenfeld, A. H. (1988). When good teaching leads to bad results: The disasters of "well-taught mathematics courses". *Educational Psychologist*, 23, 145-166.

"If the 'bottom line' is error-free and mechanical performance, students come to believe that that is what mathematics is all about."

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How My Students Responded

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The Practices in CCSS-M

- ☐ Make sense of problems and persevere in solving them.
- ☐ Reason abstractly and quantitatively.
- ☐ Construct viable arguments...
- ☐ Model with mathematics
- ☐ Use appropriate tools strategically
- ☐ Attend to Precision
- ☐ Look for and make use of structure
- ☐ Look for and express regularity in repeated reasoning.

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| KNOW | INTERACT | CREATE |
|--|---|---|
| <p style="text-align: center;">Know / Do</p> <p>Something that could be asked on a multiple choice test.</p> <p>What the student needs to know in order to do the interact piece.</p> | <p style="text-align: center;">Interact</p> <p>Something that could be answered with a short answer or paragraph.</p> <p>Which one? Why?</p> | <p style="text-align: center;">Create</p> <p>Something the student does without help from the teacher.</p> <p>Students with questions will be directed back to the interact section.</p> |

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KNOW

The slope of the line is:

a. $m = 2$
 b. $m = -2$
 c. $m = -\frac{1}{2}$
 d. $m = \frac{1}{2}$

Khan Academy

YouTube

Thatquiz

GeoGebra

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INTERACT

This is a rough sketch of 3 runners' progress in a 400 meter hurdle race. Imagine that you are the race commentator. Describe what's happening as carefully as you can. You do not need to measure anything accurately.

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KNOW

- Over a 10 day period, the amount of propane in a tank that stores propane for heating a home decreases from 461 gallons to 439 gallons. What is the rate of change (slope) of the gas in the tank?
 a. $\frac{2}{11}$ b. $\frac{11}{2}$ c. $-\frac{11}{2}$ d. $\frac{2}{11}$
- At a speed of 45 yards per minute, a 125-pound swimmer burns 110 calories in 38 minutes. Which data table could model the number of calories burned?
 a.

| | |
|-----|-----|
| y | x |
| 0 | 0 |
| -19 | 55 |
| -35 | 110 |

 b.

| | |
|-----|----|
| y | x |
| 0 | 0 |
| 15 | 19 |
| 150 | 38 |

 c.

| | |
|-----|-----|
| y | x |
| 0 | 0 |
| 15 | -19 |
| 110 | -38 |

 d.

| | |
|----|-----|
| y | x |
| 0 | 0 |
| 15 | 55 |
| 38 | 110 |
- Over a 24 second period, the amount of petrol in an airplane's tank increases from 48 gallons to 62 gallons. Which graph could model the amount of propane in the tank?
 a.
-

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INTERACT

Match each line in the graph with a column from the spreadsheet data.

Find the speed of each runner between 10 & 15 seconds and between 55 and 60 seconds.

| Time | Distance | | |
|------|----------|-----|-----|
| | A | B | C |
| 0 | 0 | 0 | 0 |
| 5 | 80 | 85 | 25 |
| 10 | 80 | 70 | 80 |
| 15 | 80 | 105 | 75 |
| 20 | 120 | 105 | 100 |
| 25 | 180 | 105 | 125 |
| 30 | 200 | 145 | 175 |
| 35 | 200 | 145 | 200 |
| 40 | 240 | 145 | 200 |
| 45 | 240 | 145 | 225 |
| 50 | 280 | 205 | 250 |
| 55 | 310 | 235 | 285 |
| 60 | 340 | 245 | 300 |
| 65 | 345 | 245 | 385 |
| 70 | 380 | 245 | 400 |

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KNOW

- According to the data table below, what is the average rate of change (slope) of the students at Harrison High School during this time period?

| Years from School | Students |
|-------------------|----------|
| 0 | 700 |
| 9 | 1147 |

a. $\frac{3}{109}$
 b. $\frac{3}{109}$
 c. $\frac{109}{3}$
 d. $\frac{109}{3}$
- In 1974, there were 19.3 million U.S. households with cable television. In 1991, there were 41.8 million U.S. households with cable television. Over that time period, which graph could model the number of U.S. households with cable television?
 a.
-

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INTERACT

You are a coach for the three runners in this race. Write two bullet points for each runner to improve their race.

| Time | Distance | | |
|------|----------|-----|-----|
| | A | B | C |
| 0 | 0 | 0 | 0 |
| 5 | 80 | 85 | 25 |
| 10 | 80 | 70 | 80 |
| 15 | 80 | 105 | 75 |
| 20 | 120 | 105 | 100 |
| 25 | 180 | 105 | 125 |
| 30 | 180 | 145 | 175 |
| 35 | 200 | 145 | 200 |
| 40 | 240 | 145 | 200 |
| 45 | 240 | 145 | 225 |
| 50 | 280 | 205 | 250 |
| 55 | 310 | 235 | 285 |
| 60 | 310 | 235 | 310 |
| 65 | 345 | 245 | 385 |
| 70 | 380 | 245 | 400 |

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| |
|--|
| CREATE |
| Record notes about your travel to school for 4 days. Pick two that have significant differences. |
| For each of the two trips you choose, make a graph, data spreadsheet, and describe in a paragraph. |
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| |
|--|
| Scale Factor & Similarity |
| Create – Choose one of the three projects |
| Price Comparison Choose a product that comes in at least three sizes. Compare the scale factor of the area or volume to the scale factor of the prices. Write a report on your findings. Paragraph headings for the report are: <i>Introduction:</i> What did you choose. Why did you choose it? <i>Hypothesis statement:</i> What do you think the outcome will be? <i>Methodology:</i> What did you do. Where did you get your data? How did you verify measurements? <i>Data:</i> What did you find out? Make a table comparing the scale factors. <i>Conclusion:</i> What is the better buy? When would the worse buy be a good option? Report must be typed and printed. You may use a report format or a powerpoint format with each paragraph represented by a slide. |
| Car Scale Drawing |

| |
|--|
| Scale Factor & Similarity |
| Know / Do |
| Watch this video on similarity and proportions. Get the packet from the files. Complete the worksheet on scale factors and similarity. Create a spreadsheet to find scale factors, and use the spreadsheet to check your work on the worksheet. Watch this video for directions. Complete the worksheet on scale factor, area, and volume. |

| |
|---|
| Scale Factor & Similarity |
| Create – Choose one of the three projects |
| Car Scale Drawing Choose your favorite car. (A field trip to a car dealership could be arranged.) Take at least 15 measurements, then use a spreadsheet to convert the measurements to a smaller scale. Using the smaller scale, make a poster-sized perspective drawing of your car. Color it with pencils or markers. Building Model Choose a room in the ALC building. Take at least 15 measurements and use a spreadsheet to convert them to a small scale. Use cardboard or foam board to create a 3-D model of the building. |

| |
|--|
| Scale Factor & Similarity |
| Interact |
| Find the diameter and price of similar pizzas from the same pizza place. Make a presentation that clearly shows the scale factor of the diameter, the scale factor of the area, and the scale factor of the price of each pizza. Come to a conclusion of which pizza is a better buy. Make a scale drawing. The drawing must be clearly labeled and include the scale factor used. Choose one: Find a picture and create an enlargement using graph paper or lined poster board. Choose a room in the school and create a scale drawing of the room using graph paper or lined poster board. |