

# Operations with Rational Numbers: Not Just the Rules 

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Think about your instruction or the mathematics program you use. What opportunities do the students have to use a variety of models to solve problems, understand concepts, or generalize ideas about fractions?

| What models are used in the program or in the classroom? |  |
| :--- | :--- |
| Area | Set |
| $\square$ Part to whole | $\square$ Part to whole |
| $\square$ Equivalence, comparing, ordering | $\square$ Equivalence, comparing, ordering |
| $\square$ Operations | $\square$ Operations |
| Number Line | Summary - In this program models ... |
| $\square$ Part to whole | $\square$ are never used |
| $\square$ Equivalence, comparing, ordering | $\square$ are sometimes used |
| $\square$ Operations | $\square$ permeate instruction |
|  |  |

Are students provided with the opportunity to...
Answer questions in which models are $\quad$ Use manipulatives to solve problems? given?

| $\square$ Never | $\square$ Never |
| :--- | :--- |
| $\square$ Occasionally | $\square$ Occasionally |
| $\square$ Throughout | $\square$ Throughout |
| Use student drawn models to solve | Use models to help develop concepts or |
| problems? | generalize ideas? |
| $\square$ Never | $\square$ Never |
| $\square$ Occasionally | $\square$ Occasionally |
| $\square$ Throughout | $\square$ Throughout |

Are there adjustments that I need to make to my instruction to assure that students experience a variety of models? If yes, describe.

## Name That Fraction

Locate the fraction $\frac{7}{8}$ on the number line below.
Starting at 0, can you reach $\frac{7}{8}$ in seven jumps? What size jumps did you make? List them here.

Starting at 0, can you reach $\frac{7}{8}$ in five jumps? What size jumps did you make? List them here.

Can you do this a different way? How?
Starting at 0, can you reach $\frac{7}{8}$ in four jumps? What size jumps did you make? List them here.

Can you do this a different way? How?
Starting at 0 , can you reach $\frac{7}{8}$ in one jump? What size jump did you make? List it here.


## Red Light-Green Light



Who is winning the Red-light, Green-light race? Here is the fraction of the distance covered from the start by the racers.

| Mary: $\frac{3}{4}$ | Harry: $\frac{1}{2}$ | Larry: $\frac{5}{6}$ | Han: $\frac{5}{8}$ | Miguel: $\frac{5}{9}$ | Angela: $\frac{2}{3}$ |
| :--- | :--- | :--- | :--- | :--- | :--- |

1. Predict.
a. Who do you think is winning?
b. Who can you rule out?
2. Explain how you decided who is winning the race:
3. Place each person in their approximate place along the race track:
4. More people arrive to play. Assign a fractional distance to how far they have traveled based on this information:
a. Alicia is between Harry and Han. $\qquad$
b. Benjamin is between Larry and Angela $\qquad$
c. Corey is between Han and Miguel. $\qquad$
Based on Teaching Student Centered Mathematics (2 ${ }^{\text {nd }}$ Edition) Activity 12.2, p. 209 (Gr. 3-5); Activity 8.1, p. 108 (Gr. 6-8), developed by Jennifer Bay-Williams.

## Adding Fractions

Matt, Sam, and Carmen each added the numbers $\frac{3}{4}$ and $\frac{3}{8}$.

|  | Does the method for adding fractions make sense? Why or why not? Explain. |
| :---: | :---: |
| Matt's Method: <br> "I halved $\frac{1}{4}$ then added." $\begin{aligned} & 1-\frac{1}{4}=\frac{3}{4} \\ & \frac{1}{8}+\frac{1}{8}=\frac{1}{4} \\ & \frac{1}{8}+\frac{1}{8}+\frac{1}{8}+\frac{1}{8}+\frac{1}{8}+\frac{1}{8}+\frac{3}{8}=\frac{9}{8} \end{aligned}$ |  |
| Sam's Method: <br> "I broke apart the $\frac{3}{8}$ to get an easier number." $\begin{aligned} & \frac{3}{4}+\frac{1}{4}=1 \\ & \frac{1}{8}+\frac{2}{8}=\frac{3}{8} \\ & 1+\frac{1}{8}=1 \frac{1}{8} \end{aligned}$ |  |
| Carmen's Method: <br> "I found common denominators." $\begin{aligned} & \frac{3}{4} \times \frac{2}{2}=\frac{6}{8} \\ & +\quad \frac{3}{8} \\ & \frac{9}{8}=1 \frac{1}{8} \end{aligned}$ |  |

## Resources

A Focus on Fractions, Bringing Research to the Classroom. Marjorie M. Petit, Robert E. Laird, and Edwin L. Marsden. Routledge. 2010.

Connecting Arithmetic to Algebra: Strategies for Building Algebraic Thinking in the Elementary. Susan Jo Russell, Deborah Schifter and Virginia Bastable. Heinemann. 2011.

Developing Essential Understanding of Rational Numbers, Grades 3-5. Carne Clarke, William Fisher, Rick Marks, Sharon Ross, Rose Mary Zbiek. NCTM. 2010

Elementary and Middle School Mathematics: Teaching Developmentally (8th Edition)
(Teaching Student-Centered Mathematics. John A. Van de Walle, Karen S. Karp and Jennifer M. Bay-Williams. Pearson. 2012.

Extending Children's Mathematics: Fractions \& Decimals: Innovations In Cognitively Guided Instruction. Susan B. Empson and Linda Levi. Heinemann. 2011.

Putting Essential Understanding of Fractions into Practice in Grades 3-5. Kathryn Chval, John Lannin, Dustin Jones, Barbara Dougherty. NCTM. 2013.

