Reasoning about Fractions: Using Number Lines to Understand Fraction Comparison

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2013 NCTM Regional Conference Las Vegas, NV



We will discuss:

- Relevant CCSS Standards and other recommendations
- Models, activities, and online resources to help students reason and compare fractions on the number line.

Some of the CCSS "Big Ideas (Clusters) in Grades 3 – 5: Number and Operations—Fractions

- Develop understanding of fractions as numbers (gr. 3)
- 2. Extend understanding of fraction equivalence and ordering (gr. 4)
- 3. Use equivalent fractions as a strategy to add and subtract fractions. (gr. 5)

More about CCSS

- Greater emphasis on using the number line model to represent and act on fractions. For example (Gr. 3 CCSS):
 - Represent a fraction I/b on a number line diagram by defining the interval from 0 to I as the whole and partitioning it into b equal parts. (3.NF.2.a)

Improving Fractions Instruction

Help students recognize that fractions are numbers and that they expand the number system beyond whole numbers. Use number lines as a central representational tool in teaching this and other fraction concepts from the early grades onward.

Developing Effective Fractions Instruction for Kindergarten through Eighth Grade: A Practice Guide (Siegler, Carpenter, Fennell, Geary, Lewis, Okamoto, Thompson, & Wray, 2010).

Considerations

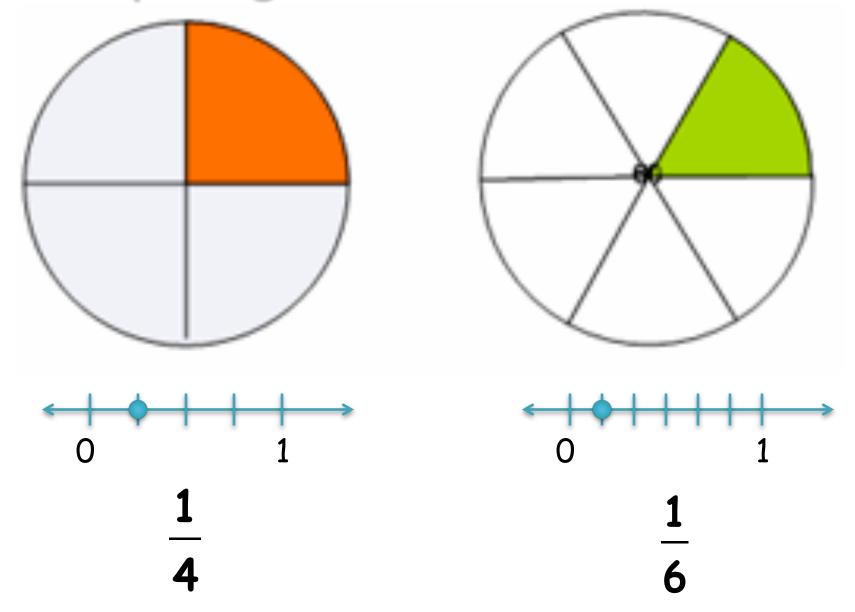
- Most children need to use concrete models over extended periods of time to develop mental images needed to think conceptually about fractions
- Students who don't have mental images for fractions often resort to whole number strategies

(Post, et al. 1985, Cramer, et al. 1997)

Types of Models for Fractions

- Area/region
 - Fraction circles, pattern blocks, paper folding, geoboards, fraction bars, fraction strips/kits
- Set/discrete
 - Chips, counters, painted beans
- Linear
 - Number lines, rulers

Comparing Fractions with a Model



One Fifth-Grader's Understanding of Comparing Fractions

Circle the larger number or write "=" if they are equal in the pairs below:

$$\frac{1}{6}$$
 $\frac{1}{3}$

1.
$$\frac{1}{7}$$
 $\frac{2}{7}$

2.
$$1 \frac{4}{3}$$

5.
$$\frac{3}{10}$$
 $\frac{1}{2}$

$$\frac{3}{6}$$
 $\frac{1}{2}$

6.
$$\frac{1}{2}$$
 $\frac{4}{6}$

One Fifth-Grader's Understanding of Comparing Fractions

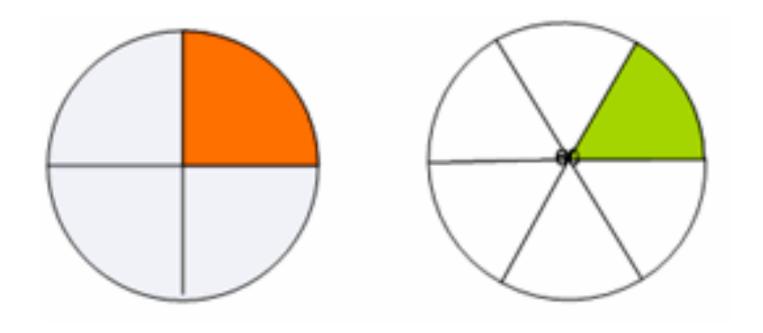


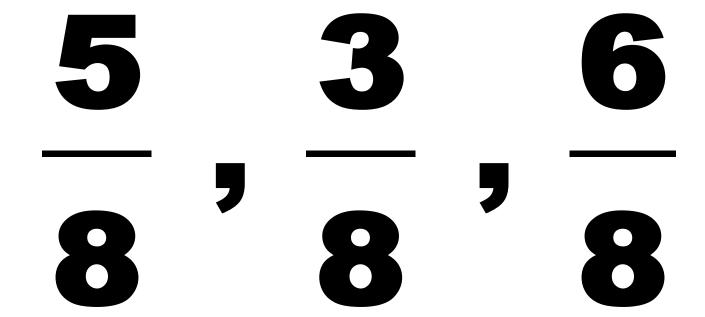
When comparing 1/6 and 1/3:

- According to Ally, "I/3 is bigger, because if you change the digit down from 3, if it was I/I it would be equal to I and one's a whole number so it's bigger".
- What does she understand and what is she struggling to understand about comparing fractions?

Think about the Language of Comparison

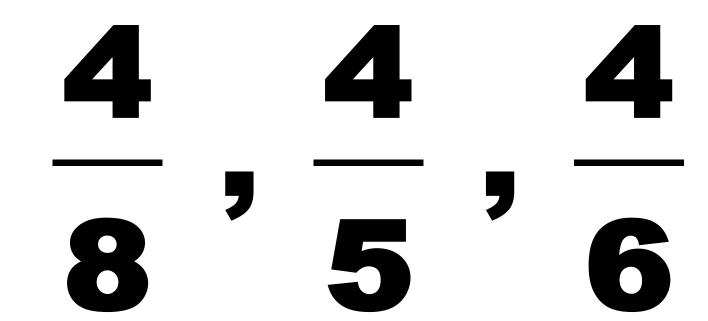
Should we use "Bigger" or "Greater"?
 (or "Smaller" or "Less than"?)



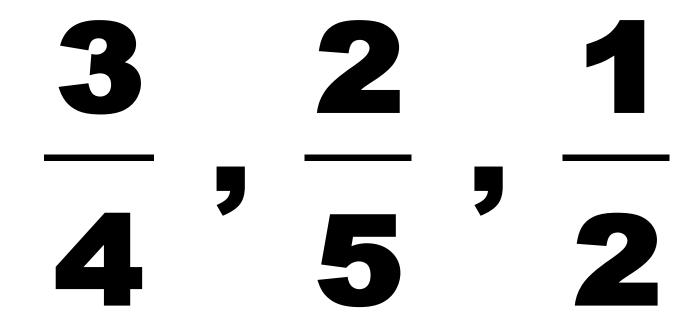


Fractions with the same denominator have the same-sized pieces, so the numerators tell which fraction has more pieces (and is greater).

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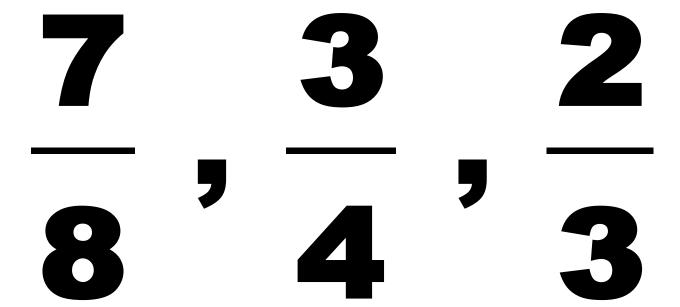
Fractions with the same numerator have the same number of pieces, and the denominators tell us which pieces are larger (and which fraction is greater).



Fractions close to a benchmark (such as ½ or 1) can be compared by finding their distance from the benchmark.

Fractions Equivalent to One-half

The denominator is twice the value of the numerator, so it's equal to 1/2



Fractions close to one can be compared by finding their distance from one, for example, by focusing on the amount that's missing from the whole.

 $\frac{99}{100}, \frac{6}{7}, \frac{15}{16}$

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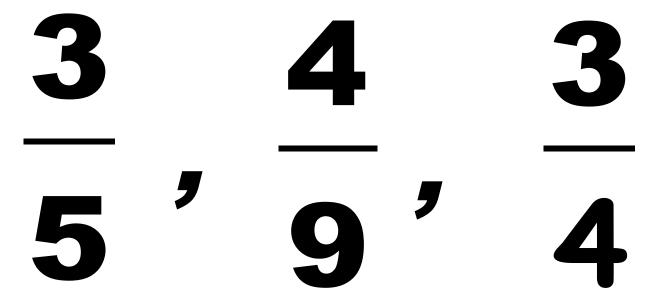
Ordering Fractions on a Number Line: The "Clothesline" Activity

- Task:
 - Order fraction tents using a clothesline to represent a number line and
 - mathematically justify the reasons for your ordering.
- Materials: fraction tents and clothesline (string, yarn, etc.)

1 3 / 2 4

 1
 3
 5

 3
 7
 4
 8



 1
 3
 6

 4
 13
 27

Free Online Fraction Resources

ConceptuaMath
www.conceptuamath.com

Resources → Tool Library → "Try the Tools"

A Few iPad Activities for Fractions

- Number Line
- Motion Math HD
- Math Tappers: Estimate Fractions

Strengthen students' fraction reasoning by helping them:

- Develop understanding of fractions as numbers.
- Understand fraction concepts, order, and equivalence,
- Use number lines as a central representational tool (but not as the first model students use for fractions) in teaching fraction concepts from the early grades onward.
- Make "Why?", "How do you know?", "Can you explain?" classroom mantras.

Contact me: nbezuk@mail.sdsu.edu

Slides and Fraction Tents
Master are available at:
www.sdsu-pdc.org
(click on "PDC
Presentations")

