

Seeing Patterns in Daily Routines

Cultivating Mathematical Practices 7 & 8

Presenters

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Friday, April 11, 2014

NCTM Conference

New Orleans, LA

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Mathematical Practices 7 & 8

SMP #7: Look for and make use of structure.

- Look for a pattern
- See structure
- Understand how numbers and spaces are organized and put together as parts and wholes.
- Recognize similarities and differences

Mathematical Practices 7 & 8

SMP #8: Look for and express regularity in repeated reasoning.

- Recognize repeated reasoning and use it to find efficient methods for solving problems
- Look for general methods for solving problems.

SMP 7 & 8 and Daily Routines

- Daily routines are a great place to highlight mathematical patterns.
- Students can look for patterns and structure in activities they do daily.
- Seeing that structure can allow students to form generalizations and efficient approaches to solving problems.

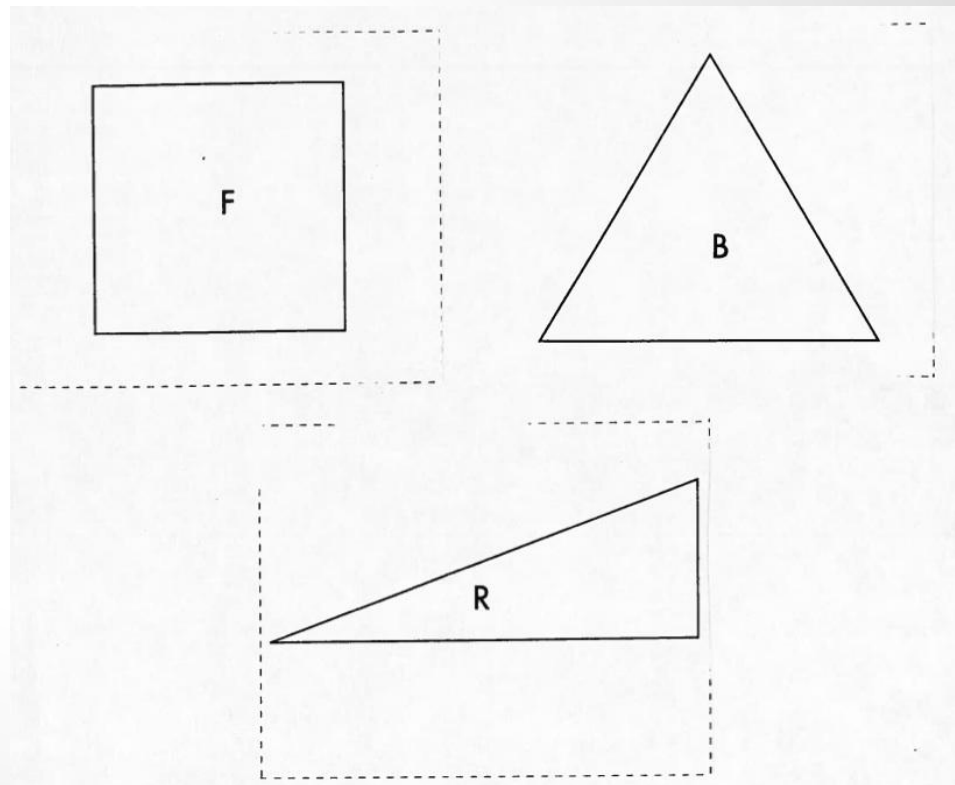
Recognize Similarities & Differences

What stays the same and what is different is a great way to help children see structure and patterns. This can be done in a variety of contexts:

- shapes
- growing patterns
- money & number sentences

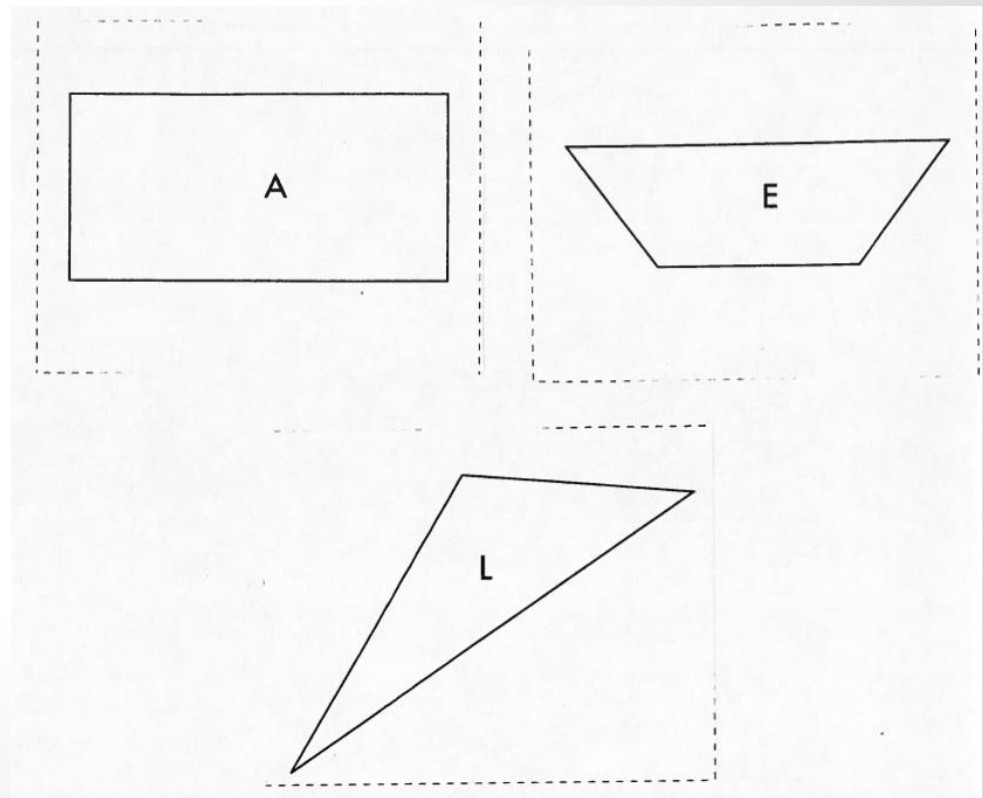
Recognize Similarities & Differences

Two are the same
One is different--



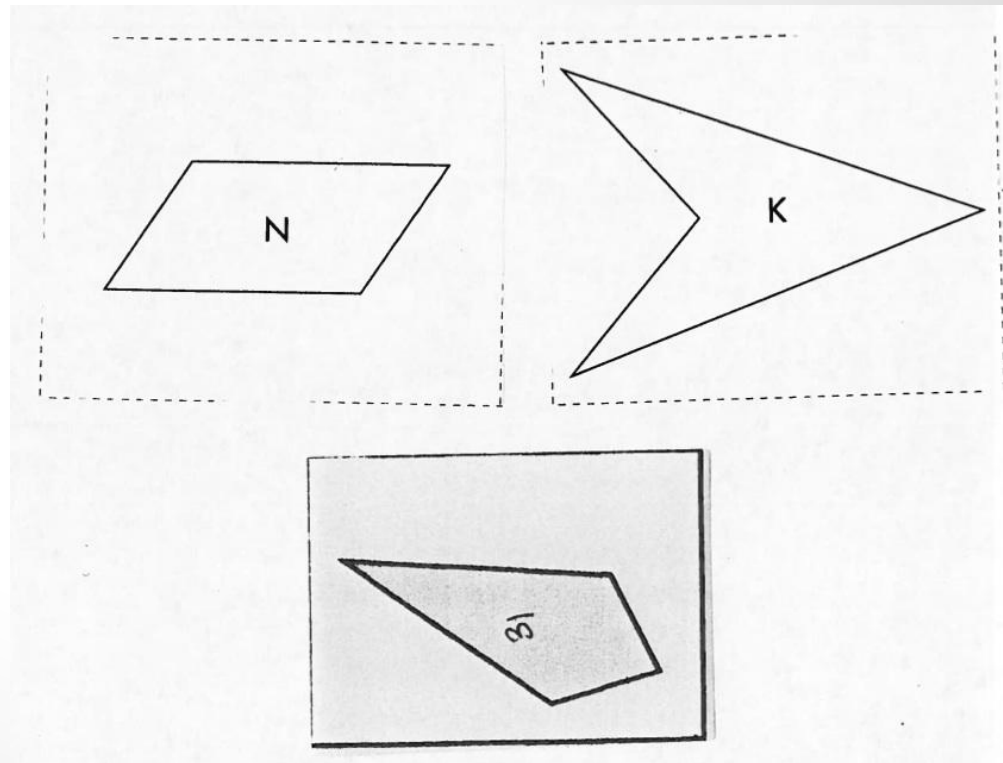
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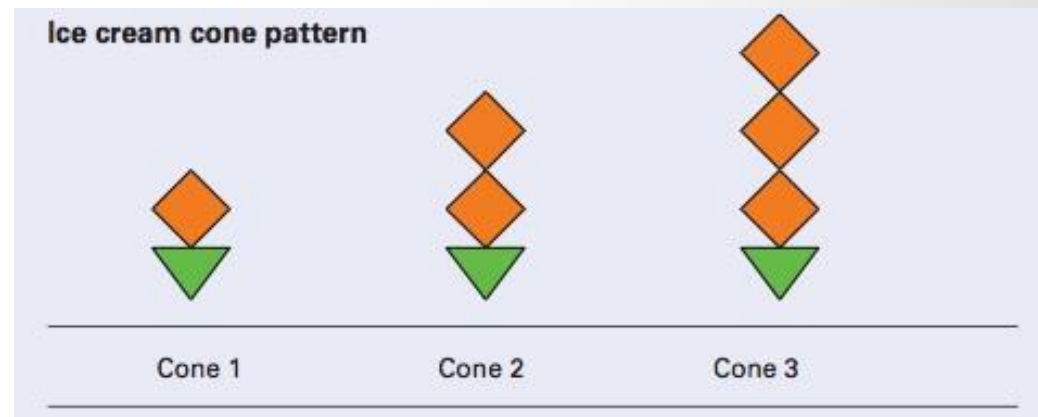
Recognize Similarities & Differences

Create your own “Two the Same, One Different” shape puzzle.

- what properties does it focus on?
- Is there more than one reasonable way to sort the shapes?

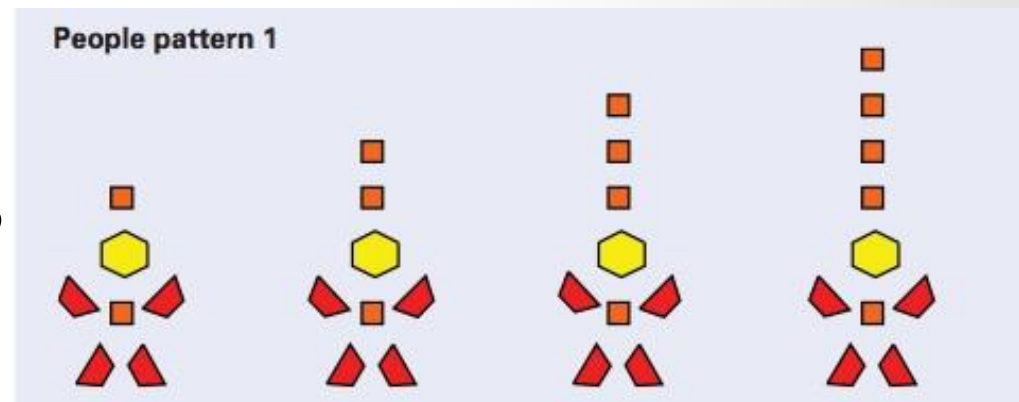
Growth Patterns

- What stays the same?
- What changes?
- How could you build the 10th cone in the pattern?



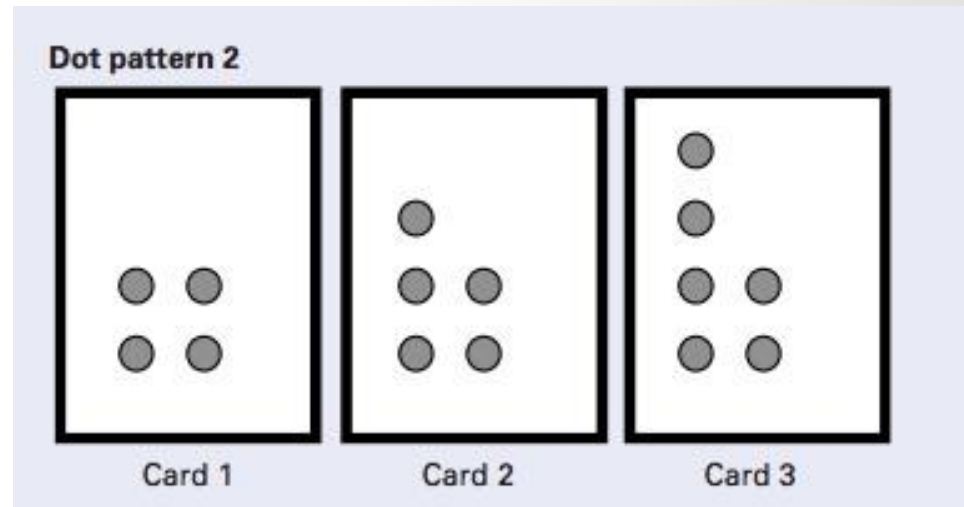
Growing Patterns

- What stays the same?
- What changes?
- How could you build the 8th person in the pattern?



Growth Patterns

- What stays the same?
- What changes?
- How could you build the 12th card in this dot pattern?



Money Trains

How can we make \$1.00 using coins?

--Compose

and

decompose

coins to make

additional

combinations

$$\begin{array}{c} \textcircled{25} \\ Q \end{array} + \begin{array}{c} \textcircled{25} \\ Q \end{array} + \begin{array}{c} \textcircled{25} \\ Q \end{array} + \begin{array}{c} \textcircled{25} \\ Q \end{array} =$$

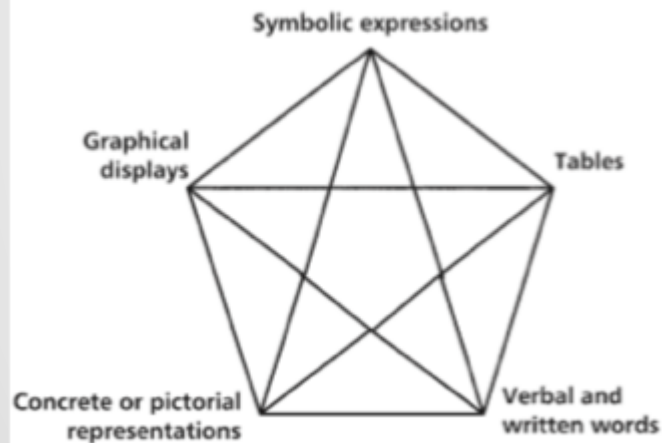
$$\begin{array}{c} \textcircled{25} \\ Q \end{array} + \begin{array}{c} \textcircled{25} \\ Q \end{array} + \begin{array}{c} \textcircled{25} \\ Q \end{array} + \begin{array}{c} \textcircled{10} \\ D \end{array} + \begin{array}{c} \textcircled{10} \\ D \end{array} + \begin{array}{c} \textcircled{5} \\ N \end{array} =$$

$$\begin{array}{c} \textcircled{25} \\ Q \end{array} + \begin{array}{c} \textcircled{25} \\ Q \end{array} + \begin{array}{c} \textcircled{25} \\ Q \end{array} + \begin{array}{c} \textcircled{10} \\ D \end{array} + \begin{array}{c} \textcircled{5} \\ N \end{array} + \begin{array}{c} \textcircled{5} \\ N \end{array} + \begin{array}{c} \textcircled{5} \\ N \end{array}$$

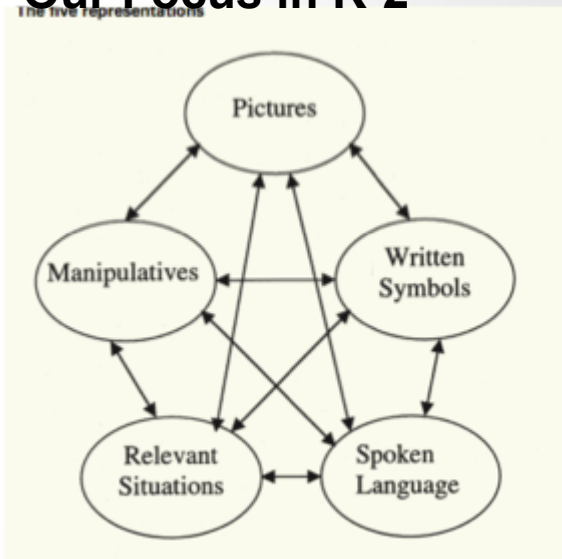
Representations (Explore Number Structure)

Representations/Models Stressed in Mathematics

(figure adapted from Friel, Rachlin, and Doyle 2001).



Our Focus in K-2



Clements, Lisa. "A Model for Understanding, Using, and Connecting Representations." *Teaching Children Mathematics*, (September 2004): 97-102.

Uses of Models/Representations

the mathematics that emerges from a model depends on what features of the model are stressed/ignored

(Mike Askew, "Models in Mind." *Primary Mathematics* (Autumn 2012):3)

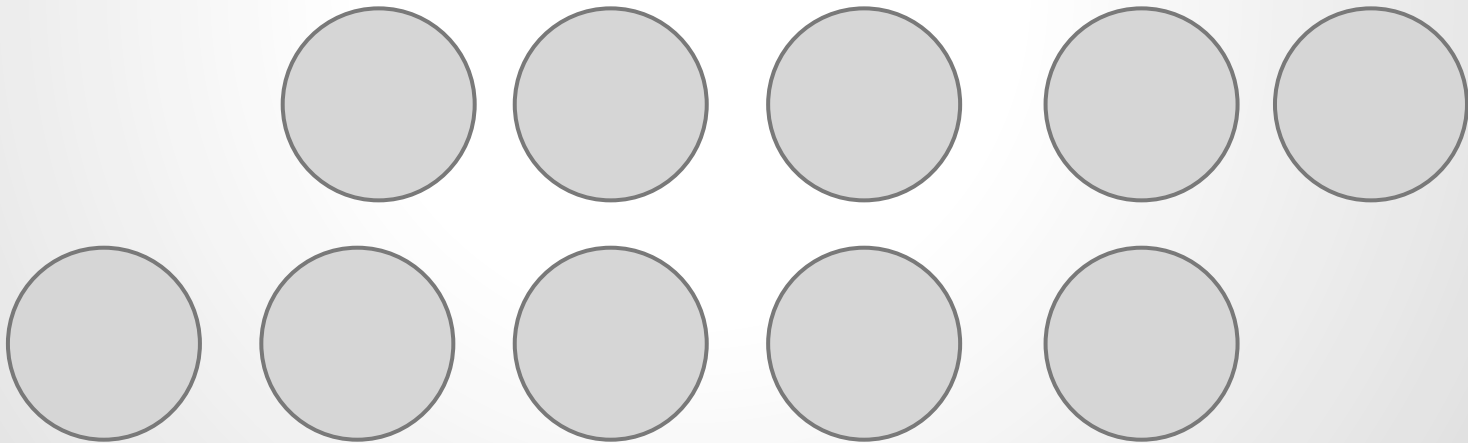
Models of Situations--Use model to help learners gain insight into mathematical structure, concepts and properties (not just getting right answers)

Models for Representing Students Strategies -- Learners may solve problems different ways and model(s) represent student thinking

Models as Tools for Thinking --the model itself become a tool for thinking/problem solving

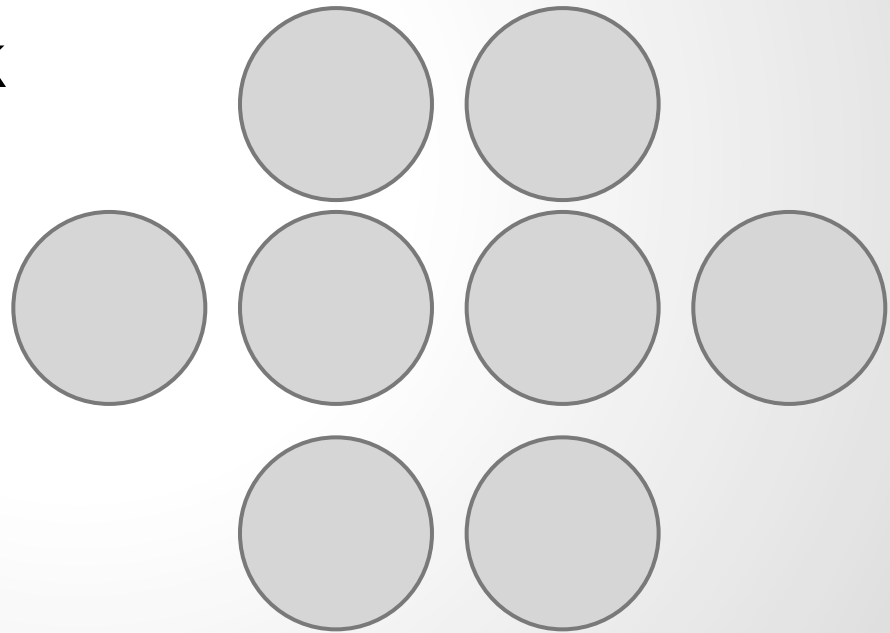
Representations - Quick Images

- How many do you see?
- How did you “chunk” the image?



Representations - Quick Images

- How many do you see?
- How did you chunk the image?



Calendar Routines

- representing a #
variety of ways
- counting on/back
- comparing

Word form

Number of the Day

Expanded form

Round to the nearest...

10 _____

100 _____

Odd or even?

10 more _____

10 less _____

100 more _____

1,000 more _____

Represent with base-10 blocks

Compare the 2 numbers

_____ ○ _____

Draw the time on the clock and write the time

_____ : _____

Represent using coins and bills

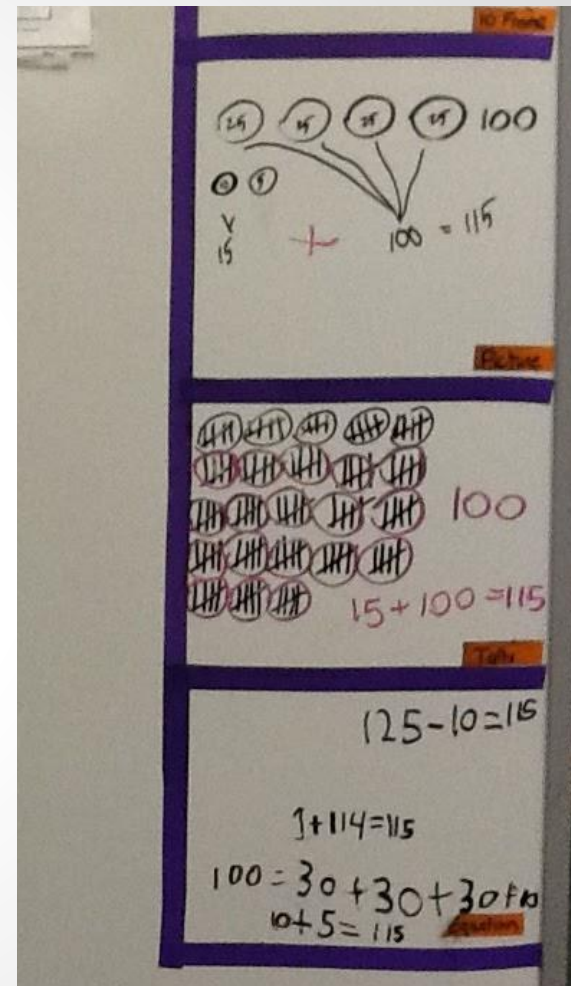
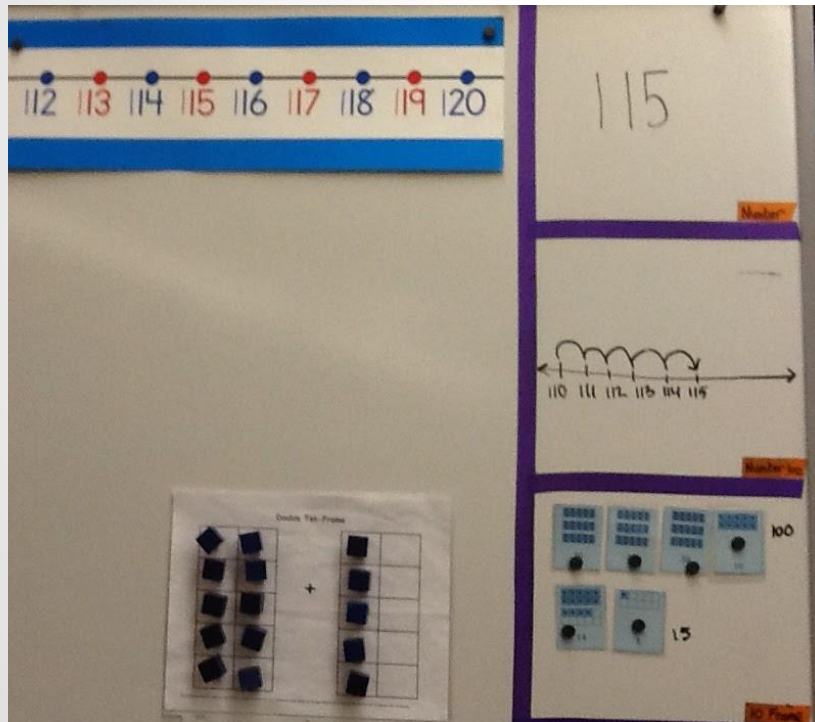
Fact family using the numbers: _____, _____, _____

Math Mountain

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Number of the Day



Number of the day - 24

How did the children use place value structure to create equivalent expressions?

How did the children use place value structure to create equivalent expressions?

Using Structure of 10 to Make 24

8+2

6+4

Other uses of structure?

[illegible]

Number Strings

What do you notice?

How are the number sentences the same?
different?

$$25 - 1$$

$$26 - 2$$

$$27 - 3$$

$$28 - 4$$

$$29 - 5$$

Number Strings

- What do you notice?
- How are the number sentences the same?
different?
- How can you use one fact to solve another?

$$5 + 5$$

$$5 + 6$$

$$3 + 7$$

$$3 + 8$$

$$4 + 6$$

$$4 + 7$$

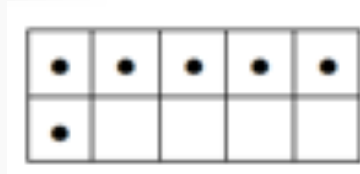
Number Strings

$$4 + 6 = \underline{\quad}$$

$$\underline{\quad} = 2 + 8$$

$$7 + 3 = \underline{\quad}$$

$$6 + \underline{\quad} = 10$$



Write as many
other 10 facts you can

- What do you notice?
- How are the number sentences the same? different?

Number Strings

- What do you notice?
- How are the number sentences the same?
different?

$$5 + 6$$

$$6 + 5$$

$$3 + 9$$

$$9 + 3$$

$$2 + 8$$

Make Your Own Number String

- What mathematical property/relationship do you want to highlight?
- What number string could you use?

Other Ideas

How else can K-2 teachers use daily routines to foster Mathematical Practices 7 & 8?

Questions or Comments?

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