



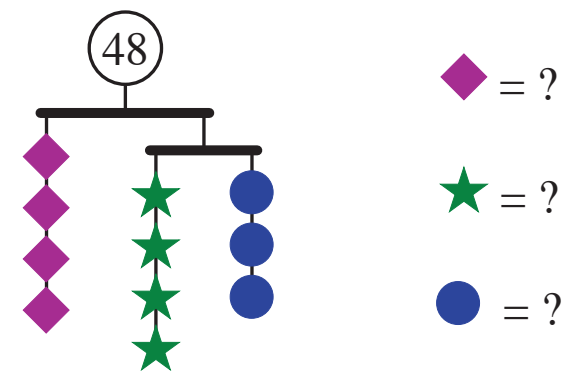
Building Puzzles

Promoting Engagement, Logical Reasoning,
and Mathematical Communication

Why Puzzles?

Mathematical Puzzles:

- are **genuine problems**
- support **number sense**
- encourage **logical reasoning**
- help students develop **strategy** in problem solving
- are **fun** and **engaging**
- promote **constructive collaboration**
- encourage **perseverance**



Who Am I? Puzzles

Who Am I?

- I am a 4-digit number.
- I am greater than 5000.
- k is my only odd digit.
- t is a square number.
- $tu = h$
- None of my digits are the same.
- The product of my digits is not 0.
- $t + 1 = k$

k	h	t	u
<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>

Who Am I? Puzzles



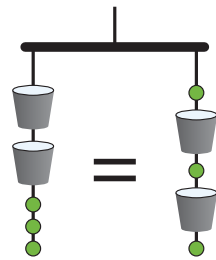
Make clues with relevant content:

- place value
- parity: evens and odds
- inequalities
- squares and roots
- multiples
- primes
- divisibility
- factors
- GCD & LCM
- algebraic expressions
- factoring (ex: $t + u = 12$ and $tu = 36$)

Mobile Puzzles: Making the logic of algebra explicit

In each of these problems a dot (•) = 1.

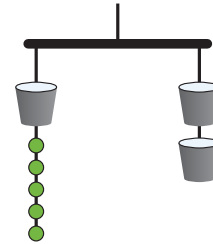
This mobile *always balances*. Why?



Equivalence

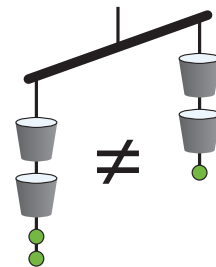
This mobile *only balances when* the buckets represent a certain number.

What number makes it balance?



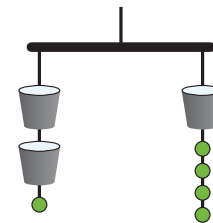
Solving

This mobile *never balances* no matter what number the bucket represents. Why?



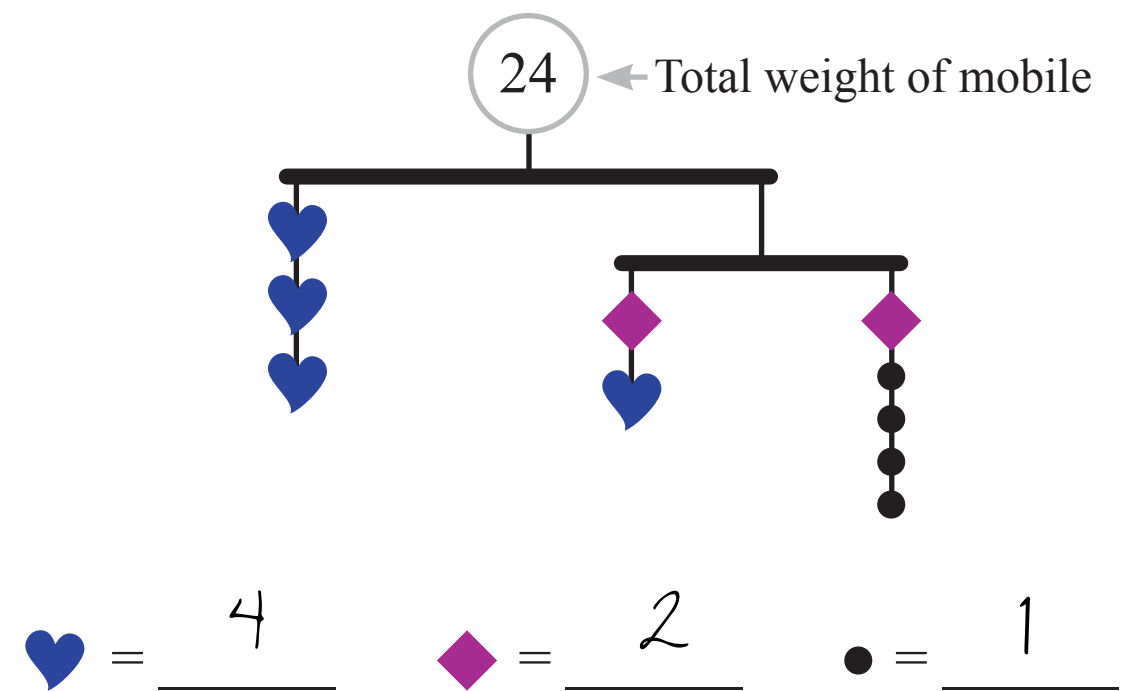
Inequality

Does this mobile balance *always, sometimes, or never*? If sometimes, *when*?

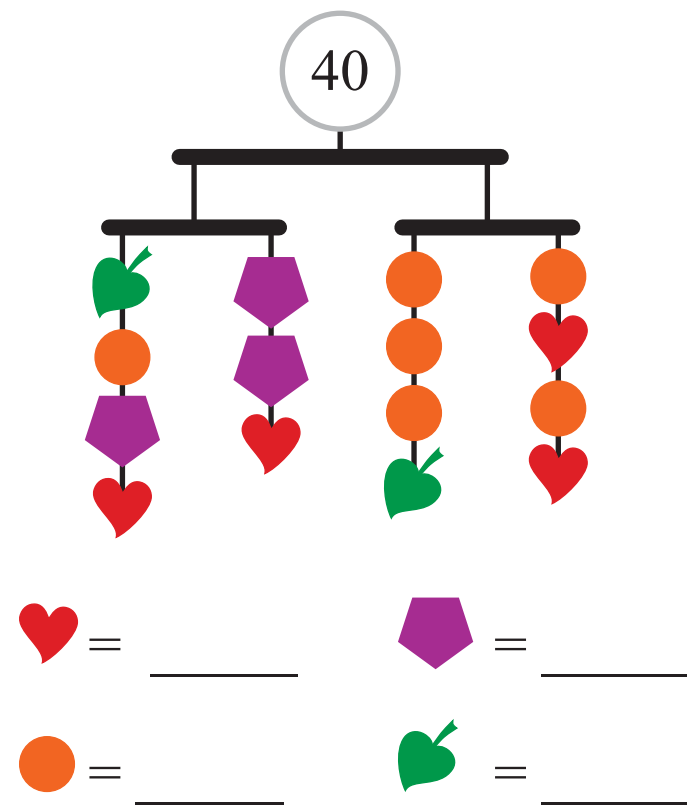


Logical Solving

Mobile Puzzles



Mobile Puzzles



$$\heartsuit + \heartsuit + \blacklozenge + \bullet = \blacklozenge + \blacklozenge + \heartsuit$$

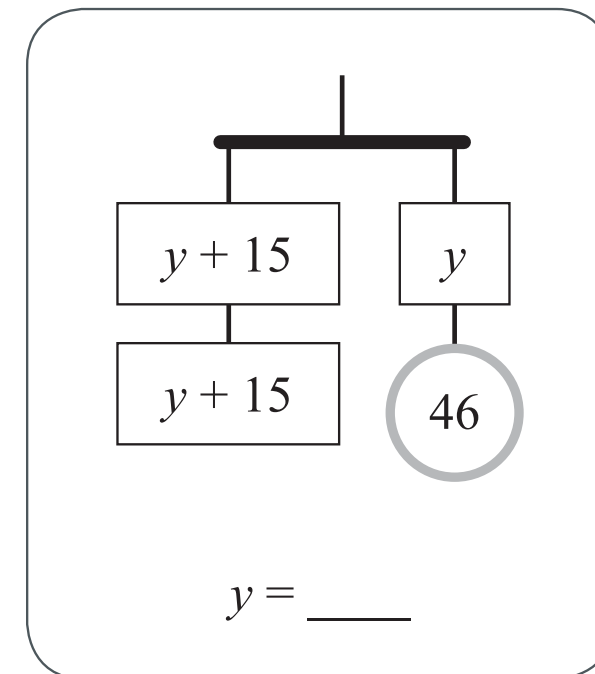
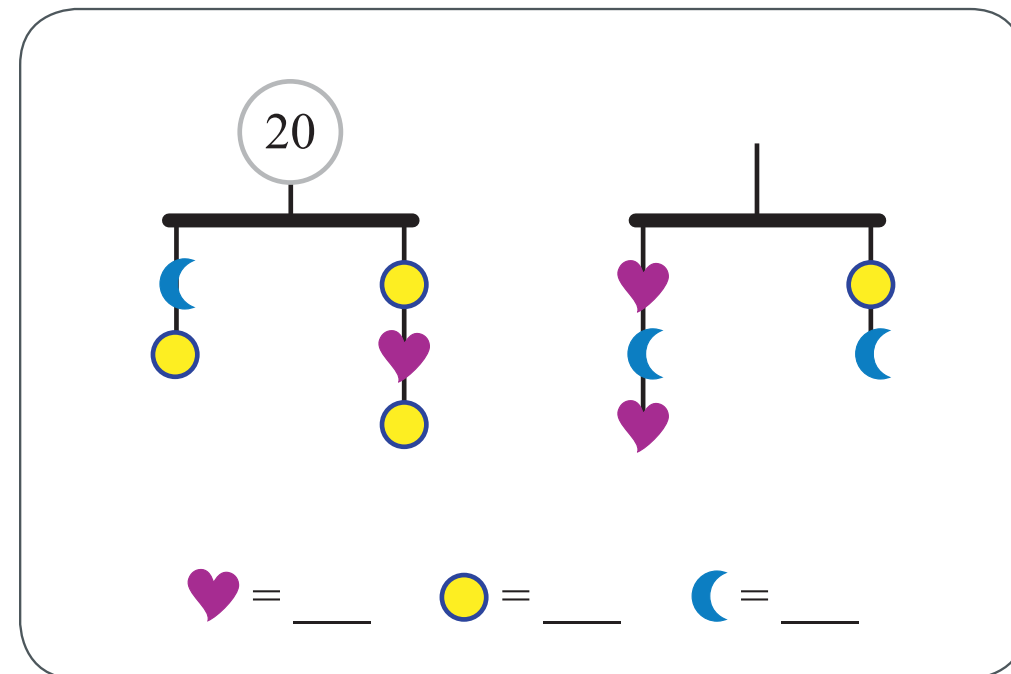
$$\heartsuit + \bullet = \blacklozenge$$

$$\bullet + \bullet + \bullet + \heartsuit = \bullet + \heartsuit + \bullet + \heartsuit$$

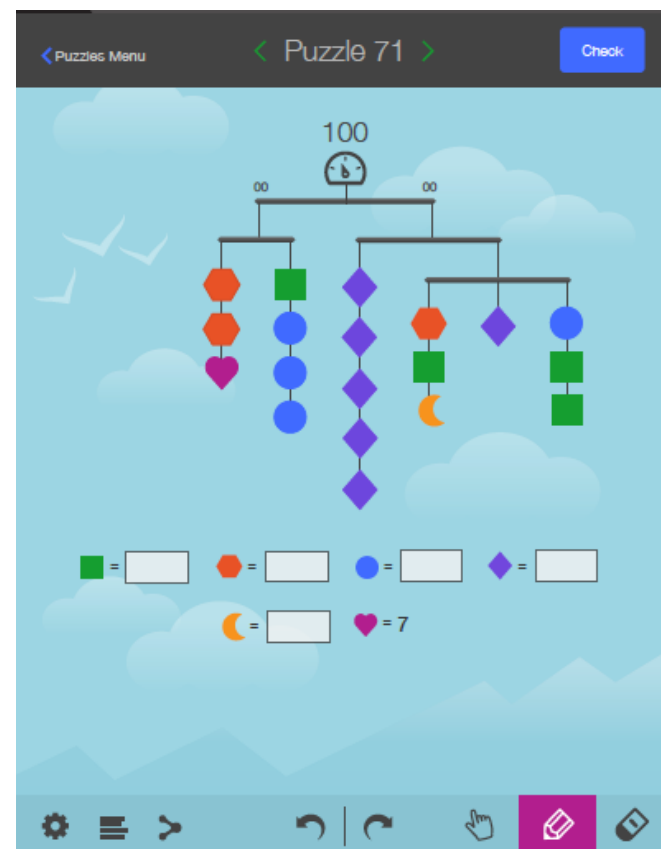
$$\bullet + \heartsuit = \heartsuit + \heartsuit$$

$$\heartsuit + \heartsuit = \blacklozenge$$

Mobile Puzzles



Mobile Puzzle App



Interactive puzzling features:

- Shape equations
- Subtraction, division, factoring
- Substitution
- Annotations
- Sharing
- “Build Your Own” mode

Latin Squares Puzzles

- Use the clues to fill in the grid so that every row and every column contains all of the elements in the title.

r, s, t Latin Square

	<i>S</i>	
		<i>r</i>

MysteryGrid Puzzles

- In MysteryGrid puzzles, the numbers in each “cage” should reach the target number using the given operation.
- For example, a 3-cell, “20, x” cage means you need to fill that cage with 3 numbers that multiply to 20.

MysteryGrid 1, 3, 4, 5

4, +		4, ÷	1, -
20, x	12, +		
			2, -
	15, x		

MysteryGrid Puzzles

MysteryGrid $2, x, 2x$

$2x+2, +$	$2x^2, \cdot$	
		$4x, \cdot$
$3x, +$		

MysteryGrid $x, 2x, 4x$

$8x^2, \cdot$	$3x, -$	
	$5x, +$	
$4x^2, \cdot$		

MysteryGrid Puzzles

MysteryGrid a, a^2, a^3, a^4

a^6, \bullet			$2a^4+a^3, +$
a^7, \bullet	a^4, \bullet		
		a^5, \bullet	
	a^7, \bullet		

Students Building Puzzles



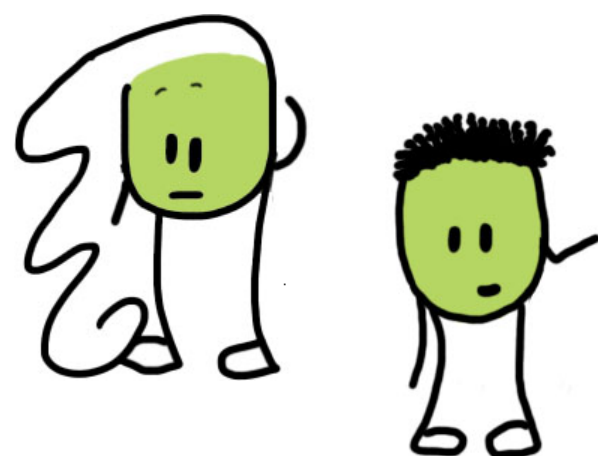
Why have students build their own puzzles?

- Supports greater **depth of understanding**
- Builds sense of **mathematical agency**

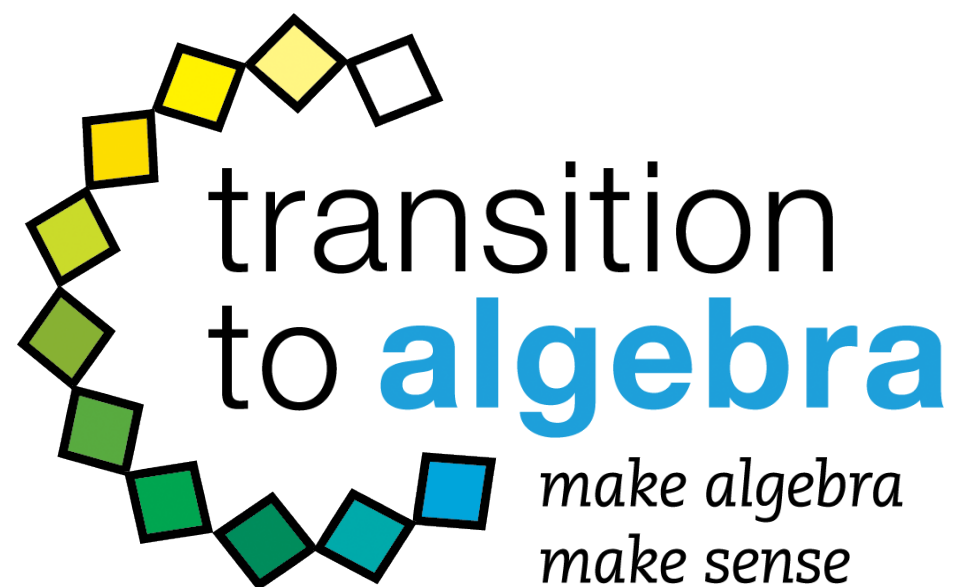
Basic strategy for creating a puzzle:

1. Design the solution first
2. Create clues
3. Check that the clues lead to a unique solution

Questions?



A Habits of Mind Curriculum



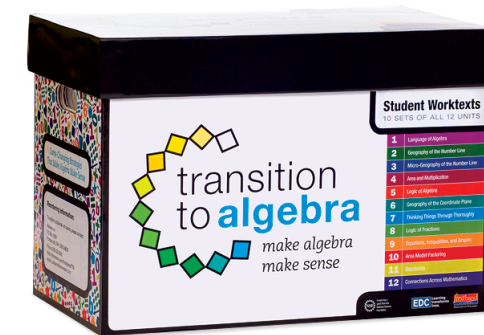
Full-year algebra-support curriculum with student & teacher materials that supports the Common Core Standards for Mathematical Practice

For more information...



- tialgebra.edc.org — theory & design principles
- transitiontoalgebra.com — materials

- Mary Fries, mfries@edc.org
- Jane Kang, jkang@edc.org
- E. Paul Goldenberg, pgoldenberg@edc.org



Problem Posing: Bringing Logic to Problem Solving for At-Risk Algebra Students



Today, 3:30 - 4:30 pm, Convention Center, R03

- Learn how to **turn problem solving into an exploratory, discussion-rich activity** through strategies such as thinking “what if not,” leaving problems headless or tailless, and presenting deductive reasoning problems.
- Change your students’ thinking from “What am I supposed to do?” into “What can I do?” and **see their perseverance and engagement rise.**