## A Multisensory Approach to Reasoning, Logic and Proof

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## Reasoning and Proof Standard

 for Grades 9-12- recognize reasoning and proof as fundamental aspects of mathematics;
- make and investigate mathematical conjectures;
- develop and evaluate mathematical arguments and proofs;
- select and use various types of reasoning and methods of proof.

| It's all about the language |  |  |
| :---: | :---: | :---: |
| conditional antecedent |  |  |
| And | disjunction | Modus Tollens |
| conjunction con | ontrapositive | consequence |
| statement | $t$ Modus | Or |
|  | Ponens | Conjecture |
| consequent |  | postulate |

## It's all about the language

conditional antecedent

## CRA Instructional Sequence

- Concrete teaches the concept
- Representational provides practice and makes memorable
- Abstract calculates with numbers and symbols


## Venn Diagrams and the Inclusive "OR"

- Do you like ice cream or lima beans?
- Do you like cabbage or candy?
- Do you like supervising lunch detention or grading exams?


## Determining Truth Values \& Truth Tables

Abstract: Analyze diagrams with numerical values

Concrete: construct diagrams using attributes of class (sports, where are our grandparents, clothing, etc )

Representational: Shade regions "and", "or", "not"

## Venn diagrams

## Conditional Statements

Language:
Conditional

Converse

Inverse

Contrapositive

## Modus Ponens and Modus Tollens

- Coding the statements aids in pattern recognition
- Code each statement ( $\mathrm{p}, \mathrm{q}, \sim \mathrm{q}$, etc) and conclusion
- Look for pattern of MP or MT


## Conditional Statements

- Construct conditional using index cards and foam
- Write out the compound sentence
- Code the sentences for $p$ and $q$
- Write in symbols
- Code and then write the truth value


| Parallel Lines and <br> Transversals |  |
| :--- | :---: |
| Interior | Exterior |
| Transversal | Alternate \& Same Side |
| Vertical | Corresponding |
| Linear Pair |  |

## It really is all about the language..

Vocabulary Development Activities
Hit my Rhombus
One more Time

Concrete: Discovering Angle Relationships


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