$$
\begin{gathered}
\text { Improve Fluency } \\
\text { and Mental } \\
\text { Strategies for Girls } \\
\begin{array}{c}
\text { Martha Carr } \\
\text { University of Georgia } \\
\text { Women and Mathematics Education }
\end{array}
\end{gathered}
$$

# Gender differences 

Young girls are less likely to be fluent
Young girls are slower to move to mental math
Why?
Not emphasized in instruction
Differences in spatial ability

# Fluency and achievement 

Fluency means that students are both fast and accurate in retrieving or calculating Fluency on basic math facts predicts improvement in strategy use and end of year math tests
Fluency frees up working memory so that students can focus on bigger/newer concepts

# Mental math and achievement 

Students who start second grade with more mental math learn more math
through the next few years
Mental math connected to fluency - can't be very fluent if counting on fingers or counters
Mental math begins with mental number line and continues with mental computation
Links to spatial ability

# Mental Number line 



Where is $57 ?$

The ability to estimate where a number is on the number line mentally is an important skill. Many students have considerable trouble doing this. Instead of estimating they typically count from the zero. This results in poor estimates.

Mental math, Arabic numbers and fluency
The better students understand Arabic numbers
the more fluent they become in computation.
They also use more advanced strategies sooner.
Need to focus on how Arabic numbers are connected on the number line.
(Vanbinst, Ghesquiere, Smedt; 2012)

## Games

Fun ways to improve fluency and mental math at home and school

# Skip-bo and other card 

## games

Students pile numbers from 1 to 10 or 12.
Need to know the next number without starting at 1
Wild cards that encourage acquisition of number
Arabic numbers used

## Card games: war

Teaches Number Magnitude
Basic or backwards
War with 2 cards
Highest sum (addition) or difference (subtraction) wins
Highest multiple wins
This may need scaffolding by other children or adults

## Games with dice encourage subitizing

## Board Games

Use games with straight sides and have students count as they move along (e.g., monopoly). Avoid board games with
curved patterns.
(see work by R. Siegler)

# Other Activities 

Team competition/ beat the teacher
Flash problem up and whole team or class calls answer
Lots of stuff on websites!
www.howtoforteachers.com/.../Maths-
Fluency-Games.pdf
Up and down the river

# Learning through testing 

Student fluency improves through repeated "testing" or repeated problem solving
Testing is not studying
Even if students get the wrong answer the action of trying to remember improves performance next time.
3 ways to test or self-test

# Massed, spaced, interleaving 

OK-
Massed - solving the same type of problem again and again

Better
Spaced - periodically testing leaving gaps in time

## Best

Interleaving of different types of problems Add, subtract, add, add, subtract

## Why interleaving?

Produces better conceptual understanding
Problems types are discriminated
Problem procedures are discriminated
Supports working memory and attention
Students require more working memory to do interleaving
Students require attention in deciding what the problem is and how it must be solved

# What can it look like in your class? 

Homework assignments - mix them up without pattern
Add, subtract, add, add, subtract
Result unknown, change unknown, start unknown
Division - measurement and partitive Multiplication, division, addition...
Cumulative tests, reviews or quizzes

## Drawbacks

Everybody thinks they do better following massed practice (not true)
You will see poorer performance when you first start interleaving
No getting around it.. It is a part of the process that pays off
Lower functioning students may have difficult time and will likely need direct instruction

## Cover, copy, compare

(Poncy, Skinner, McCallum)
Fact family triangles given to students and then covered. Students then
write subtraction using numbers
write addition using numbers
Afterwards, students compare their answers to the fact triangle Uses modeling with practice

# Final points: younger students 

Preschool and kindergarten - use numbers in language as often as possible
"Bring the 2 chairs over here"
Give verbal word problems without manipulatives
"You have 2 cookies. How many would you have if I gave you 1 more?"
Point out Arabic numbers and talk about them.
Encourage mental math once students have understanding of number.
Do they have cardinality?
Do they understand basic counting and what it means to add and subtract?

# How to encourage mental math: Older students 

Encourage students to calculate mentally Cover manipulatives and have child image them instead of counting them directly For multiplication, have students mentally skip along the number line when counting

## Final points

For fluency activities, try to make
feedback and corrections soon after mistake.
Modeling combined with practice works
best for low performing students
Ask students to write out the whole math
fact so that they learn the whole fact.
Families of problems can be used to
strengthen connections in memory

$$
\begin{aligned}
& \quad 5+2+? \\
& ?+2=7 \\
& 5+?=7
\end{aligned}
$$

Last Point
5 minutes of speeded practice for each lesson can make a difference

Even for low performing students...
Thank You!

## Questions?

