

Mary Pittman – Mathematics Content Specialist Brian Sevier- Standards Project Director

http://www.cde.state.co.us/standardsandinstruction/index.asp



Rationale/origins

From its beginnings, the field of educators across the state has been the force behind this project. This will continue to be the case as the project and its outcomes are:

- Driven by the field
- Generated by the field
- Relevant to the field

As the next step in standards support for the state, the project is oriented around three fundamental goals:

- Facilitating successful implementation of the CAS
- Helping build the capacity of Colorado educators to create curriculum materials based on the standards
- Bringing together Colorado's educators to create a variety of samples that reflect the diversity of our school districts



Project phases and major outcomes

Phase One:

Work with Colorado educators to create unit overview samples based on the CAS for all subjects and grades.

Phase Two:

 Conduct area workshops across the state to build capacity around the process and products associated with the Project

Phase Three:

 Work with Colorado educators to create units based on the overview samples for all subjects and grades based on select unit overviews



Phase One outcomes

Participants

- 500+ educator participants
- 47 of 64 counties represented
- 61 of 178 districts represented

Products

- 670 unit overviews- all content areas (k-12) and STEM (1st, 8th, high school)
- Coded to the CAS
- Teacher/educator authorship and district affiliation on every page of unit overviews

Postings

- January 31st- Standards and Instructional website-Individual content area and Sample Curriculum Project webpages
- Coming months eNet Colorado access (DREAM Marketplace)



Sample unit overviews

The Colorado Department of Education (CDE) defines curriculum as an organized plan of instruction for engaging students in mastering the standards.

The samples:

- Represent the translation of the CAS into unit overviews for all (10) content areas
- Illuminate possibilities for sequencing grade-level expectations (GLEs) and content-specific standards across courses/years
- Offer one possible foundation for exploring standards-based unit and lesson-plan development

A closer look at a Kindergarten mathematics example to:

- Highlight major components of the template
- Explain key terms
- Offer possible uses for the samples

Curriculum Development Course at a Glance Planning for Kindergarten Mathematics

	Content Area	Mathematics Grade Level Kindergarten			
	Course Name/Course Code				
	Standard Grade Level Expectations (GLE)			GLE Code	
Г	 Number Sense, Properties, 	Whole numbers can be used to name, count, represent, and order quantity			MA10-GR.K-S.1-GLE.1
ı	and Operations 2. Composing and decomposing quantity forms the foundation for addition and subtraction				MA10-GR.K-S.1-GLE.2
	 Patterns, Functions, and Algebraic Structures 	Expectations for this standard are integrated into the other standards at this grade level.			
	 Data Analysis, Statistics, and Probability 	expectations for this standard are integrated into the other standards at this grade level.			
Г	4. Shape, Dimension, and			MAID CO Y CA CLEA	
Geometric Relationships 2. Measurement is use		Measurement is used to compare and order objects	1A10-GR.K-S.	4-GLE.2	MA10-GR.K-S.4-GLE.2

Colorado 21st Century Skills



Critical Thinking and Reasoning: Thinking Deeply, Thinking Differently

Information Literacy: Untangling the Web

Collaboration: Working Together, Learning Together

Self-Direction: Own Your Learning

Invention: Creating Solutions

Mathematical Practices:

- 1. Make sense of problems and persevere in solving them.
- 2. Reason abstractly and quantitatively.
- 3. Construct viable arguments and critique the reasoning of others.
- 4. Model with mathematics.
- Use appropriate tools strategically.
- 6. Attend to precision.
- 7. Look for and make use of structure.
- 8. Look for and express regularity in repeated reasoning.

Unit Titles	Length of Unit/Contact Hours	Unit Number/Sequence
Building Block Numbers	5 weeks	Before Tricky Teens unit
Shapes all Around us	6-7 weeks	
Put it Together and Take it Apart	6 weeks	
Tricky Teens and Beyond	6 weeks	
Breaking apart is hard to do	5 weeks	After Put it Together and Take it Apart unit and Tricky Teens and Beyond unit



4. Civics	 Analyze and debate multiple perspectives on an issue
	2. The origins, structure, and functions of the Colorado gov

Colorado 21st Century Skills

His



Critical Thinking and Reasoning: Thinking Deeply, Thinking Differently

Information Literacy: Untangling the Web

Collaboration: Working Together, Learning

Together

Self-Direction: Own Your Learning

Invention: Creating Solutions

Unit Titles

Rahy Stens: From Territory to Statehood

WAID-dr.k-3.4-dec.

Mathematical Practices:

- Make sense of problems and persevere in solving them.
- Reason abstractly and quantitatively.
- Construct viable arguments and critique the reasoning of others.
- Model with mathematics.
- Use appropriate tools strategically.
- Attend to precision.
- Look for and make use of structure.
- Look for and express regularity in repeated reasoning.

Longth of Unit/Contact Hours

Unit Number/Sequence



Curriculum Development Course at a Glance Planning for Kindergarten Mathematics

Cor	ntent Area	Mathematics Grade Level Kindergarten			
Co	urse Name/Course Code				
Standard		Grade Level Expectations (GLE)			GLE Code
Number Sense, Properties,		Whole numbers can be used to name, count, represent, and order quantity			MA10-GR.K-S.1-GLE.1
	and Operations	2. Composing and decomposing quantity forms the foundation for	MA10-GR.K-S.1-GLE.2		
2.	Patterns, Functions, and Algebraic Structures	Expectations for this standard are integrated into the other standards at this grade level.			
3.	Data Analysis, Statistics, and Probability	is, Statistics, and Expectations for this standard are integrated into the other standards at this grade level.			
4.	Shape, Dimension, and	Shapes are described by their characteristics and position and created by composing and decomposing MA10-GR.K-			MA10-GR.K-S.4-GLE.1
	Geometric Relationships	Measurement is used to compare and order objects			MA10-GR.K-S.4-GLE.2

Colorado 21st Century Skills



Critical Thinking and Reasoning: Thinking Deeply, Thinking Differently

Information Literacy: Untangling the Web

Collaboration: Working Together, Learning Together

Self-Direction: Own Your Learning

Invention: Creating Solutions

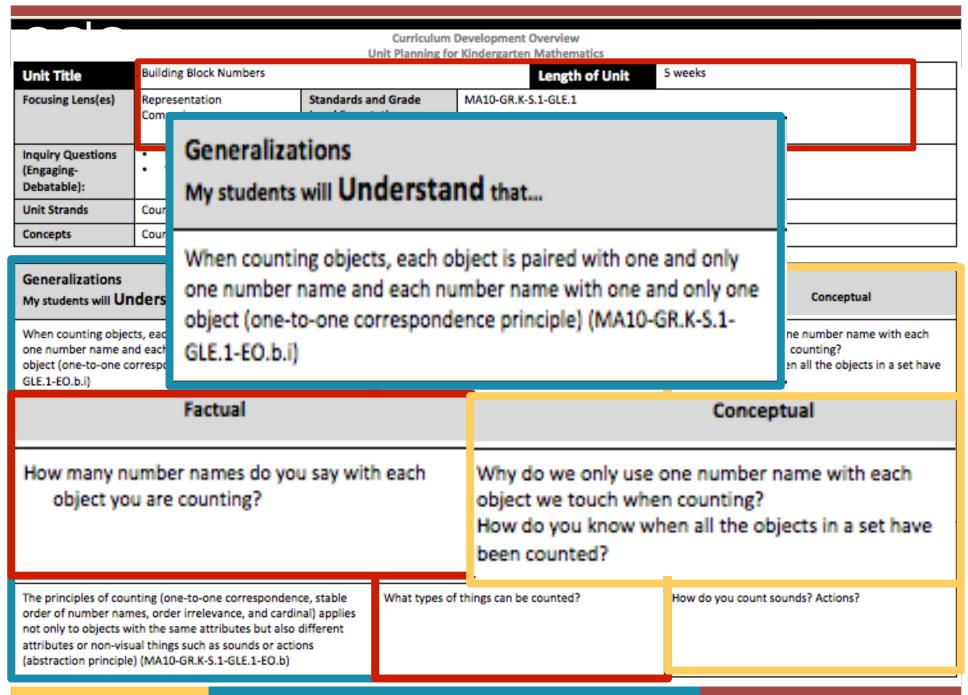
Mathematical Practices:

- 1. Make sense of problems and persevere in solving them.
- 2. Reason abstractly and quantitatively.
- 3. Construct viable arguments and critique the reasoning of others.
- Model with mathematics.
- Use appropriate tools strategically.
- 6. Attend to precision.
- Look for and make use of structure.
- 8. Look for and express regularity in repeated reasoning.

Unit Titles	Length of Unit/Contact Hours	Unit Number/Sequence
Building Block Numbers	5 weeks	Before Tricky Teens unit
Shapes all Around us	6-7 weeks	
Put it Together and Take it Apart	6 weeks	
Tricky Teens and Beyond	6 weeks	
Breaking apart is hard to do	5 weeks	After Put it Together and Take it Apart unit and Tricky Teens and Beyond unit

	Contrador Development Constant						
	Curriculum Development Overview Unit Planning for Kindergarten Mathematics						
Unit Title Building Block Numbers Length of Unit 5 weeks			Length of Unit 5 weeks				
Focusing Lens	Representation Comparison	Standards and Grade Level Expectations Addressed in this Unit	MA10-GR.K-S.1-GLE.1				
Inquiry Questions	Why do we count things? (MA10-GR.K-S.1-GLE.1-IQ.1)						
Unit Strands							
Concepts							

Generalizations My students will Un	derstand that	Guiding Factual	Questions Conceptual	
When counting object one number name a object (one-to-one of GLE.1-EO.b.i) GLE.1-EO.b.i) Generalizations My students will Understand that		e one number name with each in counting? A len all the objects in a set have		
Number names are number names print When counting thiosts, each object is paired with one and only			only one	
The last number nar the number of object many," (cardinal pri				
The principles of counting (one-to-one correspondence, stable order of number names, order irrelevance, and cardinal) applies not only to objects with the same attributes but also different attributes or non-visual things such as sounds or actions (abstraction principle) (MA10-GR.K-S.1-GLE.1-EO.b)		What types of things can be counted?	How do you count sounds? Actions?	





Key Knowledge and Skills: My students will...

What students will know and be able to do are so closely linked in the concept-based discipline of mathematics. Therefore, in the mathematics samples what students should know and do are combined.

- Count forward to 10 by ones from any given number (MA10-GR.K-S.1-GLE.1-EO.a.i., a,ii)
- Write numbers 0 to 10 as numerals (MA10-GR.K-S.1-GLE.1-EO.a.iii)
- Represent a number of objects with a written numeral with 0 representing a count of no objects (MA10-GR.K-S.1-GLE.1-EO.a.iii)
- Count as many as 10 things in a scattered configuration (MA10-GR.K-S.1-GLE.1-EO.b.ii)
- Count out a specified number of objects for quantities less than 10 (MA10-GR.K-S.1-GLE.1-EO.b.ii)
- Identify whether the number of objects in one group is greater than, less than, or equal to the number of objects in another group (MA10-GR.K-S.1-GLE.1-EO.c.i)
- Compare two numbers between 1 and 10 as written numbers (MA10-GR.K-S.1-GLE.1-EO.c.ii)
- Identify groups of objects fewer than five without counting (MA10-GR.K-S.1-GLE.1-EO.c.iii) *

EXAMPLE: A stud		he Academic and Technical vocabulary, semantics, and discourse which are particular to and necessary for accessing a given discipline. It in Language Arts can demonstrate the ability to apply and comprehend critical language through the following statement: "Mark Twain exposes the through the use of satire."		
A student in can demonstrate the ability to apply and comprehend critical language through the following statement(s):		I know there are more red bears than blue bears because I counted five red bears and three blue bears. There are ten bears and the red one is the second bear.		
Academic Vocabulary: Count, greater than, less than,		equal to, compare, objects		
Technical Vocabulary: Quantity, numeral, number, number names, zero, represent		mber names, zero, represent		

^{*}Denotes connection to Personal Financial Literacy (PFL)



Key Knowledge and Skills: My students will...

What students will know and be able to do are so closely linked in the concept-based discipline of mathematics. Therefore, in the mathematics samples what students should know and do are combined.

- Count forward to 10 by ones from any given number (MA10-GR.K-S.1-GLE.1-EO.a.i., a, ji)
- Write numbers 0 to 10 as numerals (MA10-GR.K-S.1-GLE.1-EO.a.iii)
- Represent a number of objects with a written numeral with 0 representing a count of no objects (MA10-GR.K-S.1-GLE.1-EO.a.iii)
- Count as many as 10 things in a scattered configuration (MA10-GR.K-S.1-GLE.1-EO.b.ii)
- Count out a specified number of objects for quantities less than 10 (MA10-GR.K-S.1-GLE.1-EO.b.ii)
- Identify whether the number of objects in one group is greater than, less than, or equal to the number of objects in another group (MA10-GR.K-S.1-GLE.1-EO.c.i)
- Compare two numbers between 1 and 10 as written numbers (MA10-GR.K-S.1-GLE.1-EO.c.ii)
- Identify groups of objects fewer than five without counting (MA10-GR.K-S.1-GLE.1-EO.c.iii) *

	Critical Language: includes the Academic and Technical vocabulary, semantics, and discourse which are particular to and necessary for accessing a given discipline. EXAMPLE: A student in Language Arts can demonstrate the ability to apply and comprehend critical language through the following statement: "Mark Twain exposes the hypocrisy of slavery through the use of satire."			
	A student in can demonstrate the ability to apply and comprehend critical language through the following statement(s):		I know there are more red bears than blue bears because I counted five red bears and three blue bears. There are ten bears and the red one is the second bear.	
	Academic Vocabulary: Count, greater than, less than, equal to, compare, objects			
	Technical Vocabulary: Quantity, numeral, number, number names, zero, represent			
Π	*Denotes connection to Personal Financial Literacy (PFL)			



Vocabulary: Choosing Words to Teach

	Explanation	Examples
Tier 1	•The most familiar words •Known by average 3rd grader	clock, baby, happy
Tier 2* Academic Vocabulary	High frequency words used across several content areas •Important to academic success •Not limited to one content area	coincidence, absurd, hasty, perseverance OR deconstruct, analyze, interpret, synthesize
Tier 3* Technical Vocabulary	Low-frequency words, often limited to specific content areas •Rare words •Often content-area related	nucleus, osmosis, archaeologist



Quick Terms Reference Guide

- The focusing lens brings together concepts and content for deeper thinking and meaning making
- Inquiry Questions engage students in the unit of study
- Concepts are timeless, universal, and provide a breadth of understanding
- Topics are locked in time, place, or situation (embedded in the critical content)
- Generalizations are an essential understanding that shows a relationship between two or more concepts
- Guiding questions are factual AND conceptual questions tied directly to the generalizations



- Samples:
 - The samples offer organizing structures for addressing the grade-level expectations (GLEs), evidence outcomes (EOs) and 21st century skills that build students' mastery of the standards at each grade level.
- Design reflects emphasis on concepts and content in Colorado Academic Standards
 - Centers around ideas
 - Supports teaching to greater intellectual depth
 - Emphasizes knowledge TRANSFER and APPLICATION
 - Generalizations (Big understandings) transfer
 - Concepts transfer
 - Skills transfer
- Design reflects feedback from educators across the state with technical assistance from Dr. Lynn Erickson
 - This is Colorado's Template!



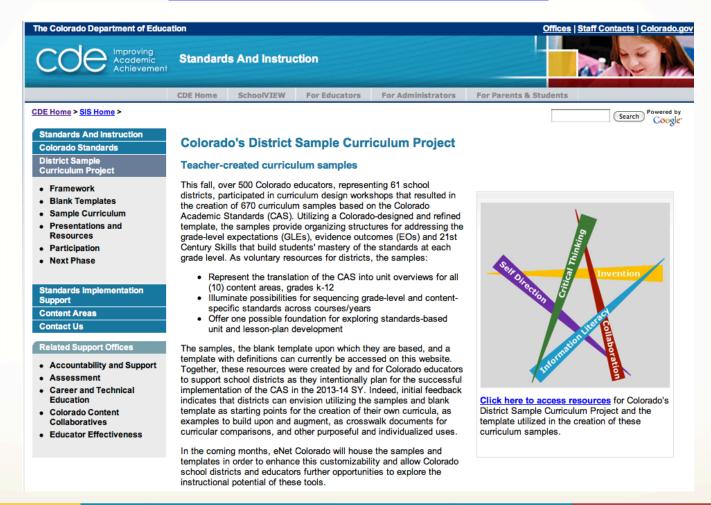
Next Steps:

Phase Three:

- Develop an instructional-unit template for all subjects and grades
- Work with Colorado educators to create unit samples for all subjects and grades based on select unit overviews
- Three-four day workshops in late July and early August
- Look for the participation application on the Standards and Instructional Support website in late spring

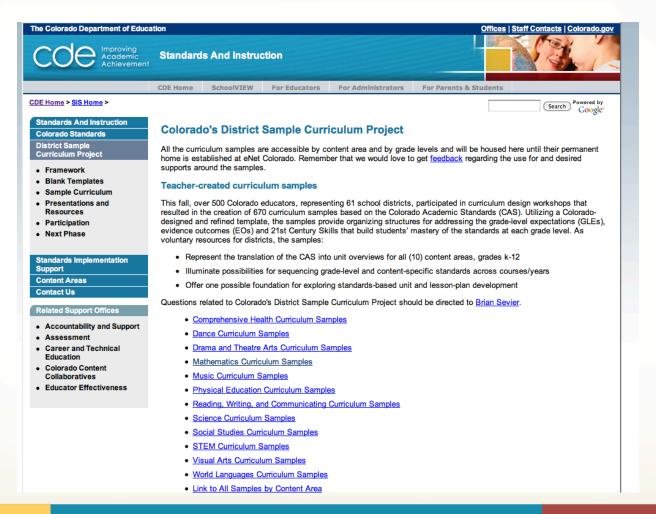


http://www.cde.state.co.us/StandardsAndInstruction/ SampleCurriculumProject.asp





http://www.cde.state.co.us/StandardsAndInstruction/ SampleCurriculum-samples.asp





http://www.cde.state.co.us/StandardsAndInstruction/Curriculum/

Mathematics.asp

CDE Home > SIS Home >

Standards And Instruction

Colorado Standards

District Sample Curriculum Project

- Framework
- Blank Templates
- . Sample Curriculum
- Presentations and Resources
- Participation
- Next Phase

Standards Implementation Support

Content Areas

Contact Us

Related Support Offices

- · Accountability and Support
- Assessment
- Career and Technical Education
- Colorado Content Collaboratives
- Educator Effectiveness

Mathematics Sample Curriculum

Initial Samples Released January 31, 2013

Google

Hello mathematics educators.

I am proud to present the k-12 mathematics curriculum samples created by Colorado educators. Working with facilitators Larry Brady (Garfield RE-2), Bev Tarpley (Cheyenne Mountain 12), Cassie Harrelson (Aspen 1), Gretchen Hazelwood (Douglas County RE 1), and Kate Canine (Poudre R-1) this past fall, over 40 educators came together to translate the Colorado Academic Standards (CAS) into curriculum.

The template upon which all of the samples are based was designed and refined by Colorado educators to highlight what students should understand, know and be able to do at the end of a given unit (detailed description of the curriculum template components). There are some unique aspects to the mathematics samples at particular grade levels, which are documented in the bullet points below.

Together, these samples are intended to support districts' transition to the CAS and the development of standards-based instructional practices by providing a voluntary resource for districts with possible options for sequencing the CAS across a course or year. Please click here to share your thoughts regarding these support resources.

Dr. Mary Pittman Math Content Specialist

Questions?: E-mail the Math Content Specialist

Update February 15, 2013. In the original posting of the Mathematics samples, we embedded what students should both know and be able to do, as a result of the teaching of a unit, in the skills section of the template. Feedback from the field, however, suggested that we specifically highlight and clarify these knowledge-skill connections. To accomplish this, we have slightly amended the "know and do" section to make the samples more accessible and user-friendly.

To learn more about the Math curriculum samples watch this presentation:





Math Samples

- High School Traditional
 - Algebra II (Word or PDF)
 - Geometry (Word or PDF)
 - Algebra I (Word or PDF)
- High School Integrated
 - Integrated 3 (Word or PDF)
 - Integrated 2 (Word or PDF)
 - o Integrated 1 (Word or PDF)
- 8th Grade (Word or PDF)
- · 7th Grade (Word or PDF)
- 6th Grade (Word or PDF)
- . 5th Grade (Word or PDF)
- 4th Grade (Word or PDF)
- 3rd Grade (Word or PDF)
- . 2nd Grade (Word or PDF)
- 1st Grade (Word or PDF)
- . Kindergarten (Word or PDF)

Unique components in the math samples::

- The unit strands for each unit overview are domains from the CCSS of mathematics.
- The Standards for Mathematical Practices are included alongside the 21st Century Skills of the Colorado Academic Standards.
- Personal financial literacy evidence outcomes for mathematics are embedded within the Key Skill sections and denoted by *.
- The PARCC Model Content Frameworks informed the creation of the unit overviews and delineation of the high school standards into both traditional and integrated course sequences.
- The learning trajectories from Turn-On CC Math supported the creation of generalizations throughout the K-8 unit overviews.

Rate this presentation on the conference app. www.nctm.org/confapp

Download available presentation handouts from the Online Planner! www.nctm.org/planner

Join the conversation! Tweet us using the hashtag #NCTMDenver