

# Teaching Computations with Fractions So Students Can Explain WHY

NCTM 2014

*Common Core* **Mathsupport.com**

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# Foamy Fractions!

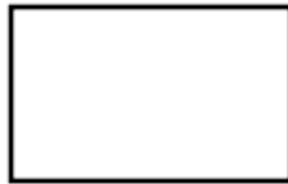
Check to make sure you have: A pair of scissors. A piece of yellow, red, orange, blue and green foam. A plastic bag, pencil or pen, and a yellow, red, orange, blue and green crayon or colored pencil.

- 1.) Pick up the yellow piece and look at it. Describe this piece. Draw a picture of the yellow piece below.

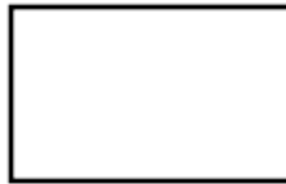
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- 2.) Pick up the red piece of foam. Is the red piece the same size as the yellow piece? \_\_\_\_\_ Follow your teacher's directions. Once finished, draw a picture of the red pieces compared to the yellow piece below.



Yellow



Red

- 3.) Each red piece is \_\_\_\_\_ out of \_\_\_\_\_ equal pieces needed to make the whole. So each red piece is called \_\_\_\_\_. Two of the red pieces would be called \_\_\_\_\_, which is the same as \_\_\_\_\_. The fractional unit of the red piece is called \_\_\_\_\_.

4.) True or False?

a.  $\frac{1}{2}$  is smaller than 1 whole. \_\_\_\_\_

By how much? \_\_\_\_\_

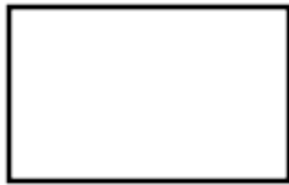
b.  $\frac{1}{2}$  and  $\frac{1}{2}$  is the same as one whole. \_\_\_\_\_

Write an equation \_\_\_\_\_

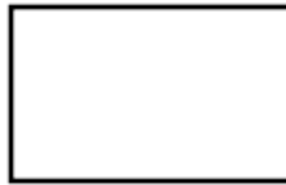
c. It takes two  $\frac{1}{2}$  pieces to make one whole. \_\_\_\_\_

Write an equation \_\_\_\_\_

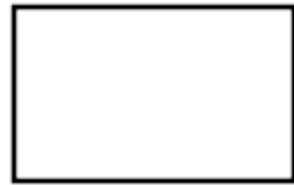
5.) Pick up the orange piece of foam. Is the orange piece the same size as the yellow piece and the red piece before you cut it? \_\_\_\_\_ Follow your teacher's directions, then draw a picture of the orange pieces compared to the yellow and red pieces below.



Yellow



Red



Orange

6.) Each orange piece is \_\_\_\_\_ out of \_\_\_\_\_ equal pieces needed to make the whole.

So each orange piece is called \_\_\_\_\_.

Two of the orange pieces would be called \_\_\_\_\_, which is equal to \_\_\_\_\_.

Three of the orange pieces would be called \_\_\_\_\_.

Four of the orange pieces would be called \_\_\_\_\_, which is equal to \_\_\_\_\_ and \_\_\_\_\_.

The fractional unit of the orange pieces is called \_\_\_\_\_.

7.) Write a true statement comparing the orange pieces to the yellow piece or the red pieces. These statements should be like those in number 4, using the fractional unit

names for the pieces. (The red is called  $\frac{1}{2}$ , two orange pieces are called  $\frac{2}{4}$ , so I could

write  $\frac{1}{2} = \frac{2}{4}$ .) Draw a picture to model the statement you write.

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8.) In a fraction, the bottom number is called the \_\_\_\_\_.

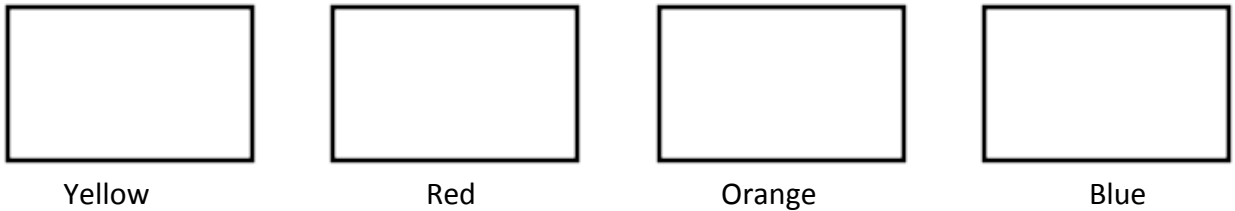
The bottom number, or the \_\_\_\_\_ tells us

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9.) A unit fraction is a fractions with a \_\_\_\_\_ equal to

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10.) Pick up the blue piece of foam. Is the blue piece the same size as the original yellow, red and orange pieces? \_\_\_\_ Follow your teacher's directions, then draw a picture of the blue pieces compared to the yellow, red, and orange pieces below.



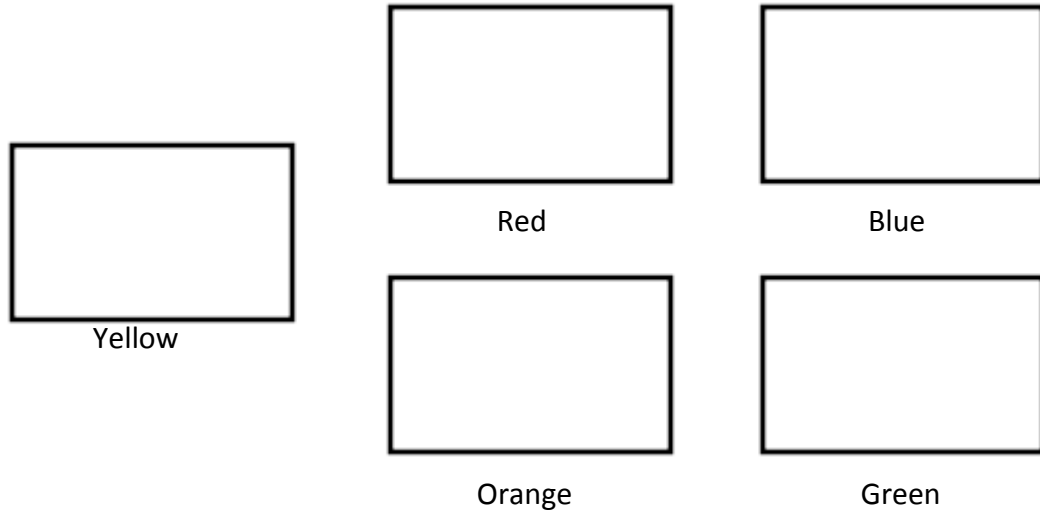
11.) Each blue piece is \_\_\_\_\_ out of \_\_\_\_\_ equal pieces needed to make the whole. So each blue piece is called \_\_\_\_\_. Two of the blue pieces would be called \_\_\_\_\_. Three of the blue pieces would be called \_\_\_\_\_, which is equal to \_\_\_\_\_, \_\_\_\_\_, and \_\_\_\_\_. The fractional unit of each blue piece is called \_\_\_\_\_.

12.) Write a true statement comparing the blue pieces to the yellow piece, red pieces or the orange pieces. Draw a picture to model your statement.

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13.) Pick up the green piece of foam. Is the green piece the same size as the original yellow, red, orange, and blue pieces? \_\_\_\_ Follow your teacher's directions, then draw a picture of the green pieces compared to the yellow, red, orange, and blue pieces below.



14.) Each green piece is \_\_\_\_\_ out of \_\_\_\_\_ equal pieces needed to make the whole. So each green piece is called \_\_\_\_\_. Two of the green pieces would be called \_\_\_\_\_, which is equal to \_\_\_\_\_. Three of the green pieces would be called \_\_\_\_\_, which is equal to \_\_\_\_\_. Four of the green pieces would be called \_\_\_\_\_, which is equal to \_\_\_\_\_. Five of the green pieces would be called \_\_\_\_\_. Six of the green pieces would be called \_\_\_\_\_, which is equal to \_\_\_\_\_, \_\_\_\_\_, \_\_\_\_\_, and \_\_\_\_\_. The fractional unit of each green piece is called \_\_\_\_\_.

15.) Write a true statements comparing the green pieces to the yellow piece or the red pieces or the orange pieces or the blue pieces. Draw a picture to model your statement.

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16.) In a fraction, the top number is called the \_\_\_\_\_. The top number, or the \_\_\_\_\_ tells us

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17.) In the fraction  $\frac{1}{2}$  the numerator is \_\_\_\_\_. It tells me \_\_\_\_\_

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The denominator is \_\_\_\_\_. It can tell me \_\_\_\_\_

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So  $\frac{1}{2}$  means I have \_\_\_\_\_ piece and the fractional unit is called

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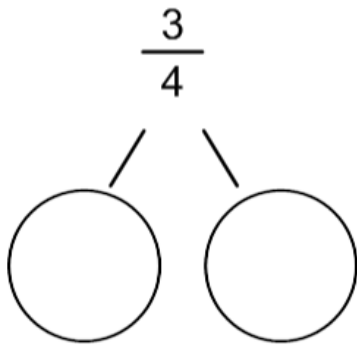
Developing the Algorithms

Composing and Decomposing  $\frac{3}{4}$

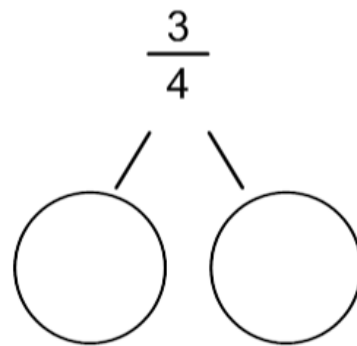
1.) Using only your fourth pieces, make the fraction  $\frac{3}{4}$ . Draw a picture below. Label each unit fraction.

2.) Using only your fourth pieces, make the fraction  $\frac{3}{4}$ . Draw a picture below. Label each unit fraction.

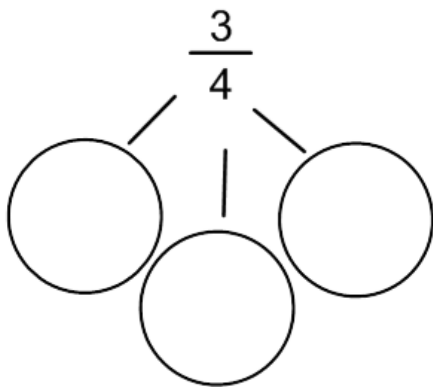
3.) Write as the sum of two addends.



4.) Write as the sum of two addends.



5.) Write as the sum of unit fractions



6.)

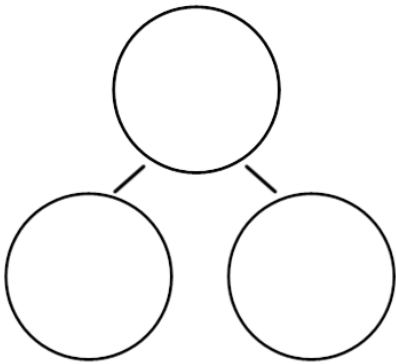
$$\frac{3}{4} = \underline{\quad} \times \frac{1}{4}$$

## Composing and Decomposing $\frac{5}{6}$

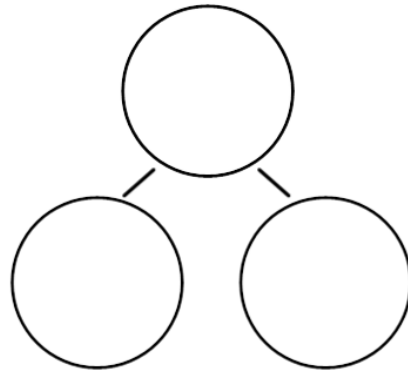
1.) Using only your sixth pieces, make the fraction  $\frac{5}{6}$ . Draw a picture below. Label each unit fraction.

2.) Using only your third and sixth pieces, make the fraction  $\frac{5}{6}$ . Draw a picture below. Label each unit fraction.

3.) Write as the sum of two addends.



4.) Write as the sum of two addends.



5.) Write as the sum of unit fractions

6.) Write an equation to show the product of a whole number and a unit fraction.

## Adding and Subtracting

$$3\frac{3}{8} + 1\frac{1}{8} =$$

Whole	Fractional unit

$$3\frac{3}{4} + 2\frac{3}{4} =$$

Whole	Fractional unit

$$3\frac{3}{4} - 1\frac{2}{4} =$$

Whole	Fractional unit

$$4\frac{3}{8} - 1\frac{5}{8} =$$

Whole	Fractional unit

$$3\frac{3}{4} + 1\frac{5}{8} =$$

Whole	Fractional unit

$$4\frac{1}{6} - 1\frac{2}{3} =$$

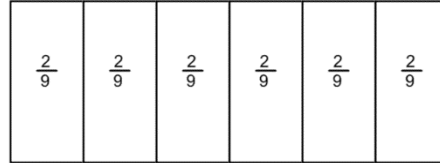
Whole	Fractional unit

## Multiplication

Write two equations (one addition and one multiplication)  
to describe this tape diagram.

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Model the following using the tape diagrams provided. Keep in mind that \* can be read as "OF".

$$8 * \frac{3}{4} =$$

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$$\frac{3}{4} * 8 =$$

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$$9 * \frac{2}{3} =$$

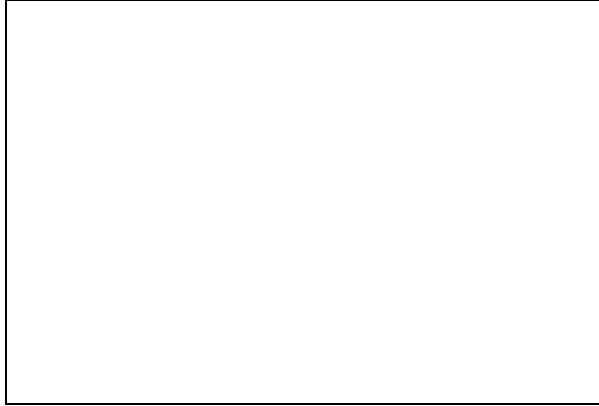
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$$\frac{2}{3} * 9 =$$

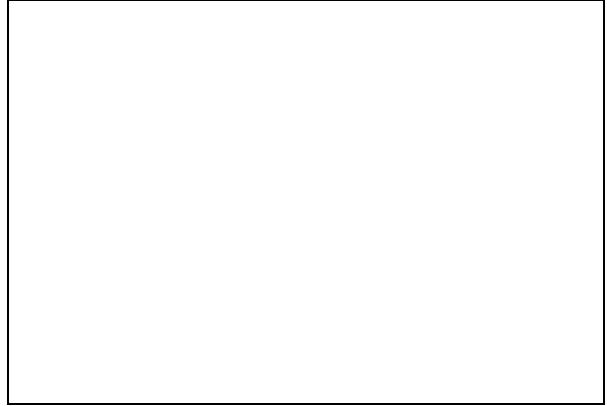
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Use your fraction pieces to solve the following. Remember, \* can be read as "OF".

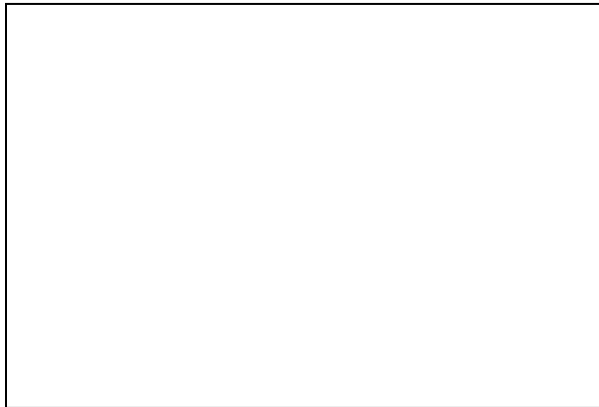
$$\frac{1}{3} * \frac{3}{8} =$$



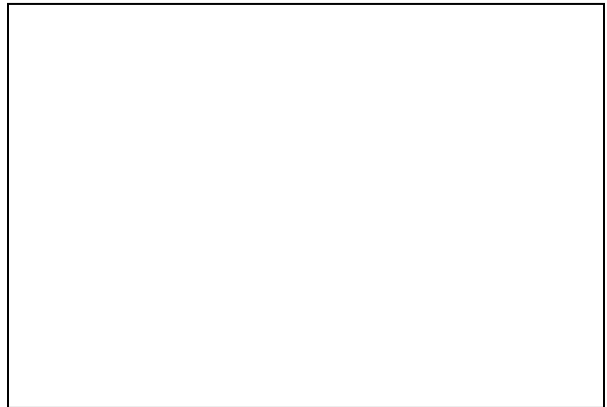
$$\frac{3}{4} * \frac{4}{6} =$$



$$\frac{2}{5} * \frac{5}{6} =$$



$$\frac{5}{6} * \frac{3}{8} =$$



$$\frac{3}{4} * \frac{2}{3} =$$

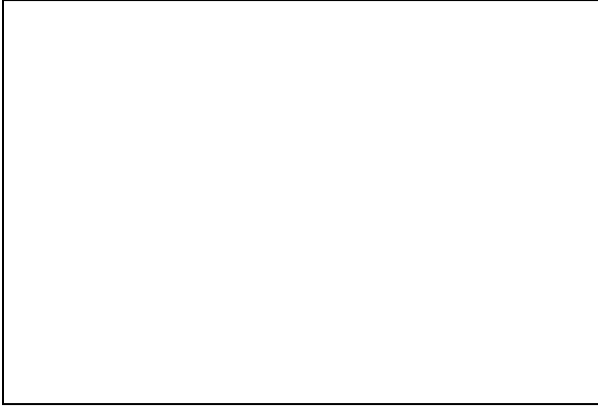


$$\frac{3}{10} * \frac{5}{6} =$$

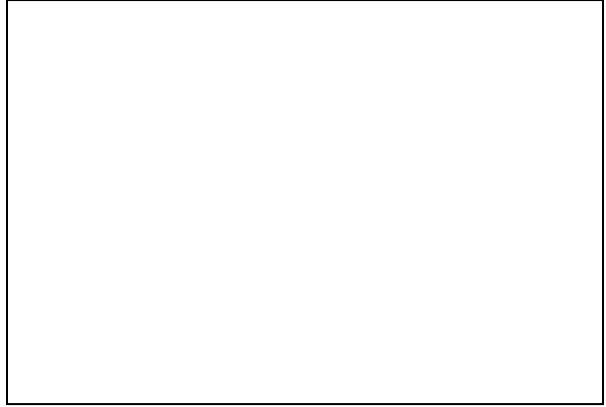


## DIVISION

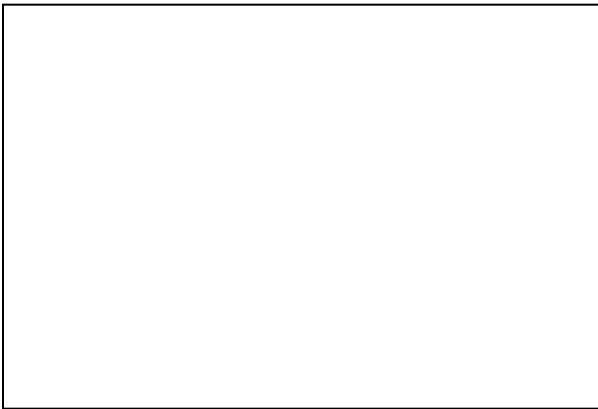
$$\frac{3}{4} \div \frac{1}{4} =$$



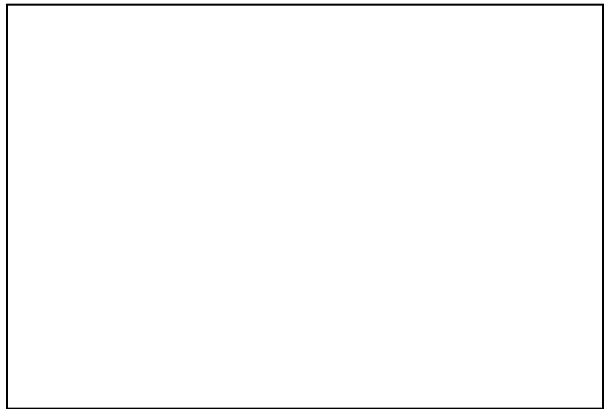
$$\frac{6}{8} \div \frac{2}{8} =$$



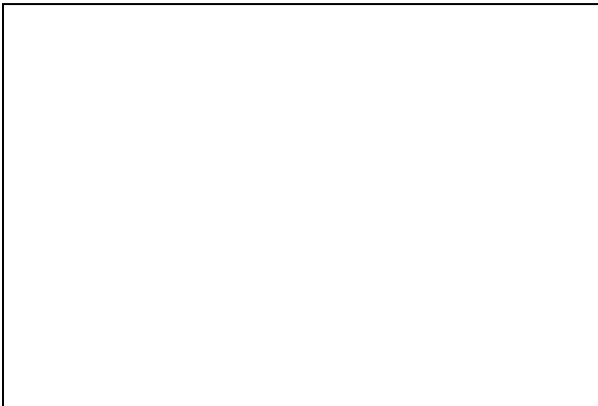
$$\frac{8}{3} \div \frac{2}{3} =$$



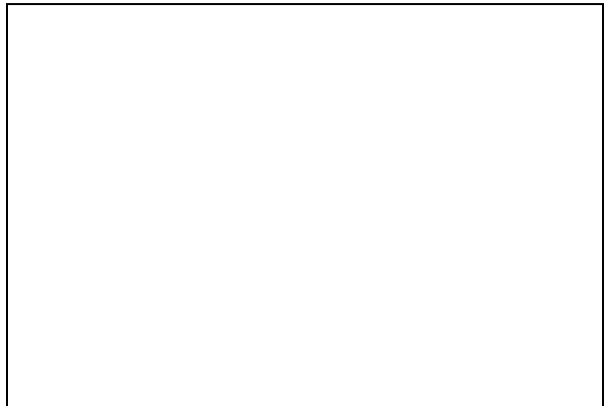
$$\frac{11}{6} \div \frac{5}{6} =$$



$$\frac{7}{4} \div \frac{3}{4} =$$

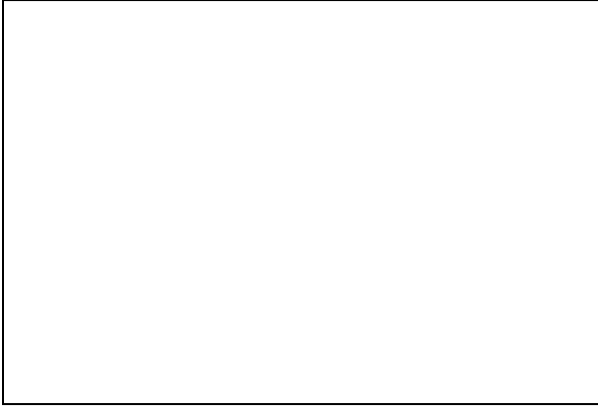


$$\frac{7}{4} \div \frac{3}{8} =$$

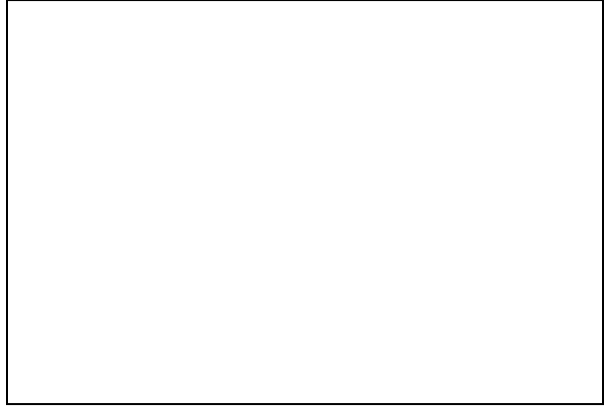


## DIVISION

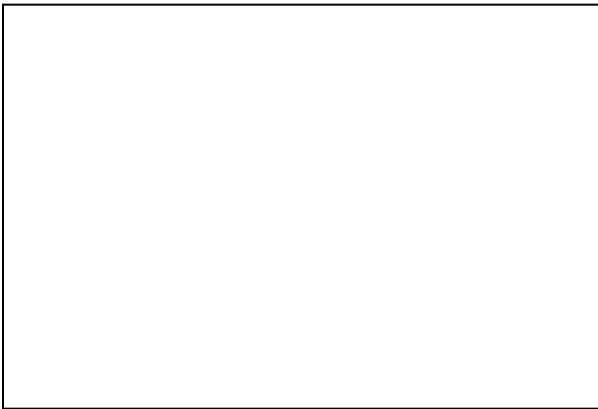
$$\frac{1}{4} \div \frac{3}{4} =$$



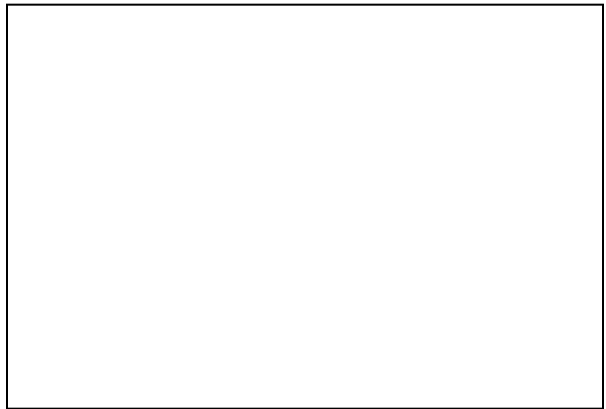
$$\frac{2}{8} \div \frac{6}{8} =$$



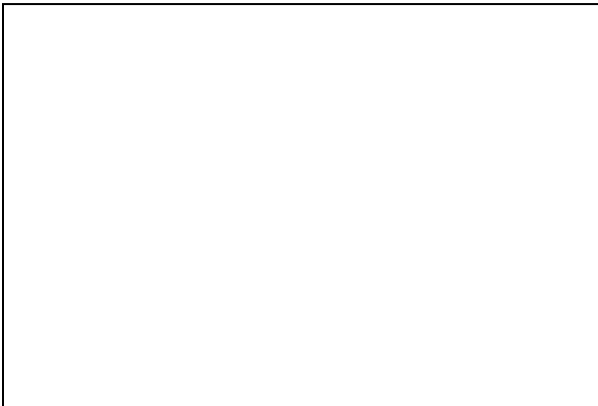
$$\frac{2}{3} \div \frac{8}{3} =$$



$$\frac{5}{6} \div \frac{11}{6} =$$



$$\frac{3}{4} \div \frac{7}{4} =$$



$$\frac{3}{8} \div \frac{7}{8} =$$

