Let's Examine Conjectures About Numbers Using Algebraic \& Geometric Reasoning


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# standards 

for
Mathematical Practice

1. Make sense of problems and persevere in solving them.
2. Reason abstractly and quantitatively.
3. Construct viable arguments and critique the reasoning of others.
4. Model with mathematics.
5. Use appropriate tools strategically.
6. Attend to precision.
7. Look for and make use of structure.
8. Look for and express regularity in repeated reasoning.

$$
\begin{array}{cc}
3+5 & 29+31 \\
5+7 & 41+43 \\
11+13 & 59+61 \\
17+19 & 71+73
\end{array}
$$

## WHY?

## CONJECTURING CAN HELP

DEEPEN UNDERSTANDING
THROUGH:
-EMPOWERING
\& BUILDING OWNERSHIP
-IMPROVING COMMUNICATION
\& REASONING SKILLS
-LEARNING FROM MISTAKES

# MAKE <br> CONJECTURES THAT ADDRESS <br> NATURAL NUMBERS WRITTEN IN TERMS <br> OF CONSECUTIVE NATURAL NUMBERS. 



| For each doodle, count V, F, E and record in table. |  | Vertices | $\begin{gathered} \mathbf{F} \\ \text { Faces } \end{gathered}$ | $\begin{gathered} \mathbf{E} \\ \text { Edges } \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: |
|  | 1. |  |  |  |
|  | 2. |  |  |  |
|  | 3. |  |  |  |
| Find a pattern. | 4. |  |  |  |
|  | 5. |  |  |  |
|  | 6. |  |  |  |
|  | 7. |  |  |  |
|  | 8. |  |  |  |
| - | 9. |  |  |  |
| $()$ | 10. | 0. |  |  |

1. 


2.


NAME: DOODLE COUNT

For each doodle, count V, F, E and record in table.

Find a pattern.


| V <br> Vertices |  | F <br> Faces | $\mathbf{E}$ <br> Edges |
| :--- | :--- | :--- | :--- |
| 1. |  |  |  |
| 2. |  |  |  |
| 3. |  |  |  |
| 4. |  |  |  |
| 5. |  |  |  |
| 6. |  |  |  |
| 7. |  |  |  |


4.

5.


# Explore: The max region count within a circle determined by 3 chords 



0-1


1-2
2-4

## Conjectures.

-On a $5 \times 5$ geoboard there are more than 50 squares.
-On a $5 \times 5$ geoboard there's a path more than 50 units long that does not intersect with itself.

- On an nxn geoboard the maximum number of interior points for a triangle is a triangular number.



## FIND THE SUM OF THE MEASURES

 $\mathbf{O F}<\mathbf{A}+<$ B $+<\mathbf{C}+<$ D $+<$ E.Conjecture about the sum of the angle measures at the tips of the 5 -, 6-, 7-, 8-pointed stars.


## References : Conjectures, The Common Core, Problem Solving

Bezuszka, Stanley J. \& Kenney, Margaret J. "Just Five Does It", Mathematics Teaching in the Middle School, Vol 12, No. 8, April, 2007.

Bremigan, Elizabeth G. "Is It Always True? From Detecting Patterns to Forming Conjectures to Constructing Proofs", Mathematics Teacher, Vol. 97, No. 2, February, 2004.
Brown, Stephen \& Walter, Marion. The Art of Problem Posing, $2^{\text {nd }}$ Edition. Hillsboro, NJ: Lawrence Erlbaum and Associates, 1990.

Burke, Maurice. "Star Rec", Student Math Notes, January 1989, Reston, VA: National Council of Teachers of Mathematics.

Cox, Rhonda L. "Using Conjectures to Teach Students the Role of Proof". Mathematics Teacher, Vol. 97, No. 1, January, 2004.

Dugdale, Sharon. Matthews, James I. \& Guerrero, Shannon. "The Art of Posing Problems and Guiding Investigations". Mathematics Teaching in the Middle School, Vol. 10, No. 3, October, 2004.

Katz, Victor J. A History of Mathematics: An Introduction, $\mathbf{3}^{\text {rd }}$ Edition. New York, NY: Addison Wesley, 2008.

Knuth, Eric J. "Fostering Mathematical Curiosity", Mathematics Teacher, Vol. 95. No. 2, February, 2002.

National Council of Teachers of Mathematics. Focus in High School Mathematics: Reasoning and Sense Making. Reston, VA: NCTM, 2009.

National Council of Teachers of Mathematics. Principles and Standards for School Mathematics. Reston, VA: NCTM, 2000.

Polya, George. How to Solve It: A New Aspect of Mathematical Method $2^{\boldsymbol{n d}}$ Edition. Princeton, NJ: Princeton University Press, (1957), 1973.

Polya, George. Mathematical Discovery: On Understanding, Learning, and Teaching Problem Solving, Volume I, New York, NY: John Wiley \& Sons, Inc., 1962.

## Common Core State Standards for Mathematics

http://www.corestandards.org/Math

