## Data and slope and y-intercepts, Oh My!

Linear Regression in the Common Core


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## Outline

I. Data collection-Cheerios
II. History lesson
III. More data collection-wire and red vines
IV. Math Chat
V. More examples and resources
VI. Technology resources

Thanks to: http://purpleprontopups.wordpress.com/ and http://statteacher.blogspot.com for sharing the correlation station ideas with me via Twitter and their blogs.

## Common Core Standards

8.SP Investigate patterns of association in bivariate data.
r. Construct and interpret scatter plots for bivariate measurement data to investigate patterns of association between two quantities. Describe patterns such as clustering, outliers, positive or negative association, linear association, and nonlinear association.
2. Know that straight lines are widely used to model relationships between two quantitative variables. For scatter plots that suggest a linear association, informally fit a straight line, and informally assess the model fit by judging the closeness of the data points to the line.
3. Use the equation of a linear model to solve problems in the context of bivariate measurement data, interpreting the slope and intercept. For example, in a linear model for a biology experiment, interpret a slope of $1.5 \mathrm{~cm} / \mathrm{hr}$ as meaning that an additional hour of sunlight each day is associated with an additional 1.5 cm in mature plant height.
S.ID Summarize, represent, and interpret data on two quantitative variables 6. Represent data on two quantitative variables on a scatter plot, and describe how the variables are related.
a. Fit a function to the data; use functions fitted to data to solve problems in the context of the data. Use given functions or choose a function suggested by the context. Emphasize linear, quadratic, and exponential models.
b. Informally assess the fit of a function by plotting and analyzing residuals.
c. Fit a linear function for a scatter plot that suggests a linear association.
S.ID Interpret linear models
7. Interpret the slope (rate of change) and the intercept (constant term) of a linear model in the context of the data.
8. Compute (using technology) and interpret the correlation coefficient of a linear fit.
9. Distinguish between correlation and causation.

## Station One

On Station One's poster, with $x$ values o-3ı and y values o-3ı, x equals the day of the month of your birthday and $y$ represents the number of days left after your birthday in your birth month.

Number of Days in each Month:

$$
\begin{aligned}
& \text { January - 3I days February - 29 days } \\
& \text { March - 3ı days } \\
& \text { May - 3ı days } \\
& \text { July - 3ı days } \\
& \text { September - 3o days } \\
& \text { November - 3o days }
\end{aligned}
$$

For example, Mr. Derksen's birthday is on January $28^{\text {th }}$ (FYI, I love doughnuts) so his point would be at:

$$
\mathrm{X}=\mathrm{L}_{\mathrm{I}}=\text { Birth day }=28
$$

$\mathrm{Y}=\mathrm{L} 2=$ Number of days left in month $=3$

## Station Two

Measure your forearm in millimeters.
Measure your forearm + your hand in millimeters.

$$
\begin{gathered}
\mathrm{X}=\mathrm{L}_{\mathbf{I}}=\text { forearm } \\
\mathrm{Y}=\mathrm{L}_{2}=\text { forearm }+ \text { hand }
\end{gathered}
$$



## Station Three

Make a circle of cheerios. Count the number it takes to make the circle. Count the number it takes to make the diameter.
$\mathrm{X}=\mathrm{LI}=$ diameter
$\mathrm{Y}=\mathrm{L} 2=$ \# around


## Station Four

Make a circle FULL of cheerios. Count the number it takes to fill entire the circle. Count the number it takes to make the radius.

$$
\mathrm{X}=\mathrm{LI}=\text { radius }
$$

$\mathrm{Y}=\mathrm{L} 2=$ total \# to make the circle


## Station Five

Roll the die. This is the number of knots you will tie in the wire. After tying the knots, measure the length of the wire in inches.

Don't forget to untie the knots before leaving this station!!

$$
\begin{gathered}
\mathrm{X}=\mathrm{L}_{\mathrm{I}}=\# \text { of knots } \\
\mathrm{Y}=\mathrm{L}_{2}=\text { length of wire } \\
\text { Station SiX }
\end{gathered}
$$

Take a bite of a red vine.
Measure the remaining piece in cm .
Weigh it.
Repeat (two data points per team)

$$
\begin{aligned}
& \mathrm{X}=\mathrm{L}_{\mathrm{I}}=\text { length }(\mathrm{cm}) \\
& \mathrm{Y}=\mathrm{L}_{2}=\text { weight }(\mathrm{g})
\end{aligned}
$$

## Station Seven

$X=L_{i}=\#$ of letters in your first name
$\mathrm{Y}=\mathrm{L} 2=$ length of the longest hair on your head (inches)

## Station Eight

$$
X=L I=\text { shoe size }
$$

$\mathrm{Y}=\mathrm{L} 2=$ length of the longest hair on your head (inches)

## Other data sets

| car | hp | mpg |
| :--- | :--- | ---: |
| Audi A4 | 211 | 30 |
| BMW 3 series | 230 | 28 |
| Buick LaCrosse | 182 | 30 |
| Chevy Cobalt | 155 | 37 |
| Chevy Suburban <br> 1500 | 320 | 21 |
| Ford Expedition | 310 | 20 |
| GMC Yukon | 320 | 21 |
| Honda Civic | 140 | 34 |
| Honda Accord | 177 | 31 |
| Hyundai Elantra | 138 | 35 |
| Lexus IS 350 | 306 | 25 |
| Lincoln Navigator | 310 | 20 |
| Mazda Tribute | 171 | 28 |
| Toyota Camry | 169 | 33 |
| Volkswagen Beetle | 150 | 28 |


|  | total <br> runs |  |
| :--- | ---: | ---: |
| Team | attendance |  |


|  | interest | amount |
| ---: | ---: | ---: |
| 1985 | 11.93 | 65.3 |
| 1986 | 10.09 | 75.5 |
| 1987 | 9.52 | 81.9 |
| 1988 | 10.04 | 82.8 |
| 1989 | 10.21 | 96.7 |
| 1990 | 10.06 | 97.4 |
| 1991 | 9.38 | 101.0 |
| 1992 | 8.21 | 104.4 |
| 1993 | 7.27 | 101.9 |
| 1994 | 7.98 | 96.1 |
| 1995 | 8.01 | 99.4 |
| 1996 | 7.81 | 107.2 |
| 1997 | 7.73 | 118.7 |
| 1998 | 7.05 | 124.9 |
| 1999 | 7.32 | 126.4 |
| 2000 | 8.14 | 129.2 |
| 2001 | 7.03 | 143.9 |
| 2002 | 6.62 | 148.9 |
| 2003 | 5.83 | 155.4 |
| 2004 | 5.95 | 158.2 |
| 2005 | 6.00 | 183.0 |
| 2006 | 6.60 | 200.3 |
| 2007 | 6.44 | 210.7 |
| 2008 | 6.09 | 213.1 |
| 2009 | 5.06 | 215.8 |
| 2010 | 4.84 | 212.6 |

(C) Pearson Education 2or3<br>Stats, Modeling the World<br>Bock, Velleman, DeVeaux

## Technology Resources

Excel
slope (y, x)
intercept $(\mathrm{y}, \mathrm{x})$
correl ( $\mathrm{x}, \mathrm{y}$ )
Statcrunch
www.statcrunch.com

## StatKey

http://lock5stat.com/statkey/index.html
Casio AP Stats Guide
http://www.casioeducation.com/educators/activities

## Texas Instruments

Make sure to go to Catalog-Diagnostic On

## NCTM

http://www.nctm.org/resources/content.aspx?id=327o6
Useful Applets
http://media.pearsoncmg.com/aw/aw_bock_statsmodel_3/cw/smw3e_references.html

## Data Sources

http://lib.stat.cmu.edu/DASL/DataArchive.html
Smarter Balanced Calculator (includes a regression tool!)
http://sbac.portal.airast.org/practice-test/calculators/
Guess My Correlation
http://istics.net/stat/correlations/

