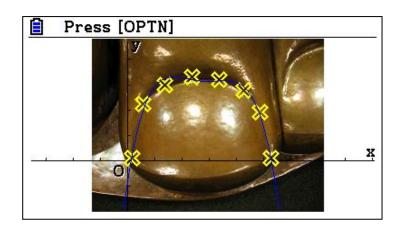
A Pedi for the Lady...

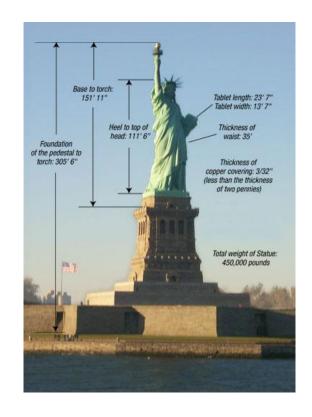
And Other Area/Volume Activities

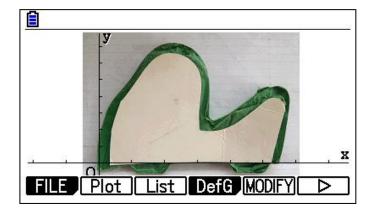
Investigations that provide a foundation for Calculus

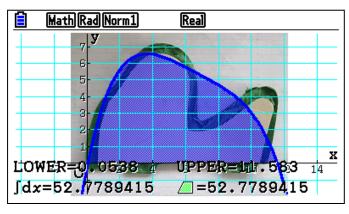
Deedee Henderson

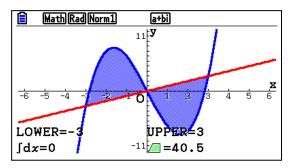
Oxford, Alabama dhenderson.oh@oxford.k12.al.us







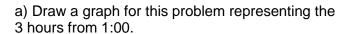




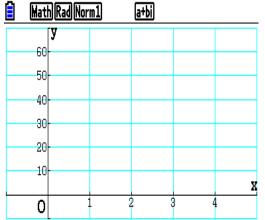
Did you know that D=RxT is connected to velocity, integration, and the area under a curve? Let's see how this simple concept is considered to be CALCULUS!

1. Texas Pete is on I-20 moving west at the rate of 60 mph. At 1:00, he presses the cruise control on the car

and then lets the car travel at this \underline{steady} rate for 3 hours.



- b) Find the area trapped between the graph and the x-axis.
- c) Describe the meaning of the area in context to this problem.
- d) Find the slope of the graph and describe its meaning with respect to the problem.

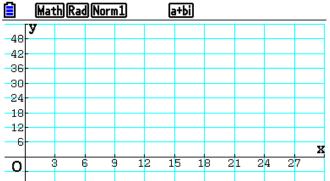


2. Professor Ben Dover is going from home to work. It is a straight path from his home to work with no stops along the way. It takes him 6 minutes to get to 48 mph. He then travels at 48 mph for 18 minutes and then it takes him another 2 minutes to some to a stop.

then it takes him another 3 minutes to come to a stop.



- b) Find the area under the curve.
- c) Determine the meaning of the area in context to the problem.



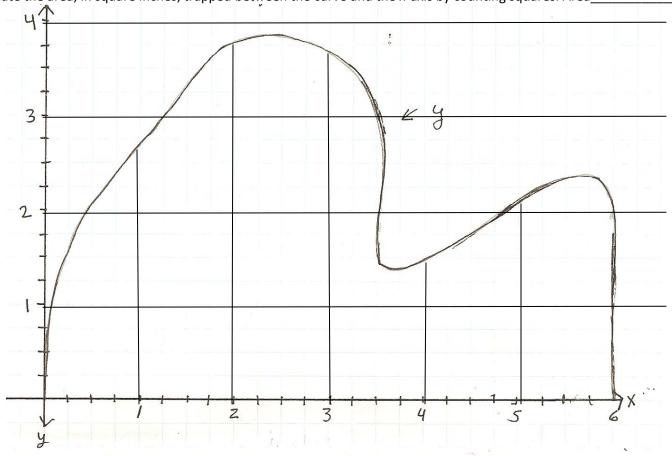
- d) Find the slope of the first six minutes and the last three minutes. What do these numbers represent?
- 3. Sasquatch is filling his hot tub with hot water using his on-demand water heater. As time passes, the hot water is dispersed more slowly. The table below states the rates at which the heater fills the hot tub at 20 minute intervals. If the hot tub initially had 10 gallons in it, how many gallons are in it at the end of 120 minutes?



Time	0	20	40	60	80	100	120
min							
Rate	50	46	46	40	35	30	20
gal/min							

Slicing a Mushroom: Finding Area and Volume Activity

1. Estimate the area, in square inches, trapped between the curve and the x-axis by counting squares. Area_____



2. Lightly color the **area** covered by using the <u>Midpoint</u> Riemann Sum Method with 6 sub-intervals, each 1-inch long. Use a different color for each rectangle. Estimate and record the area covered by this method.

3. Find the *polynomial* equation that best fits the mushroom's shape by using the regression feature of your calculator. Regression is located in the **Statistics** mode Use the points from the integer and midpoint values on the graph.

State the value and meaning of r^2 : ______. Y1=______

4. Graph the equation from step 3 using the **Graph** mode.

Find the area by "integrating" between the roots of Y1: **Area** = $\int_a^b Y1dx =$ ______

What do the roots represent in context to this graph? ______

Find the area by using this integral: **Area**: $\int_{0}^{6} Y1 dx =$

What is the significance of 0 and 6 on this integral?

5. Compare the calculations for the area. What could be done to make these estimates better?

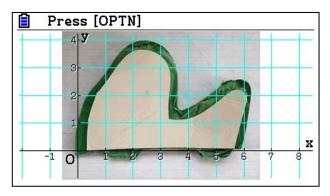
6. Now....Imagine the shape being spun about the *x-axis* in such a way that it forms a *solid*. Find the *volume* of this solid using the same 6 slices as in step 2 where the height of the graph at each <u>midpoint</u> represents the length of the radius of each cylinder.

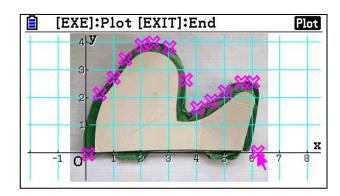
Volume of a cylinder: V=______ The **Volume** of this figure is______ by this method.

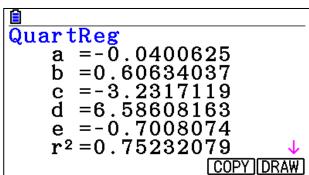
7. Using the equation from step 3, find the volume of this solid by "integrating" between the x-intercepts.

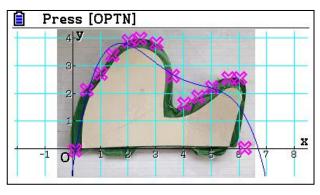
Volume=
$$\pi \int_{0}^{6} (Y1)^2 dx =$$
 ______ What does $Y1$ represent in this expression? _____

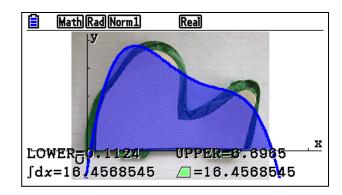
Using the Casio Picture Converter, any picture can be imported, and then many explorations can be done. Which of the following regression equations would be the best estimate of the area? Explain!

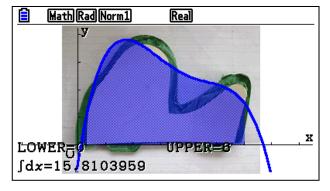








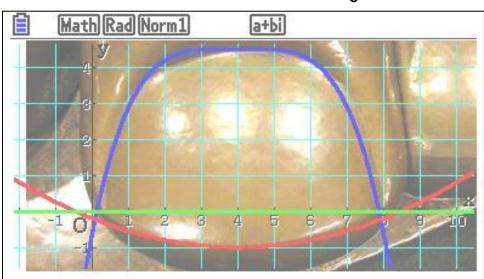




The volume could then be estimated by substituting the quartic equation into $V = \pi \int_0^\infty (Y1)^2 dx$ and calculating the integral using the **Run** mode. Based on the derived equation for Y1, the volume is approximately 145.651 cubic inches.

How does this compare to your answer in question 6?

A Pedi For the Lady



1. Estimate the area in square inches trapped above and below the QUARTIC curves outlining the shape of Lady Liberty's big toe nail by counting squares! Each unit in the picture is equivalent to about .45 feet. Round final answers to tenths place.

Area \approx _____ square <u>units</u> Convert to square feet: Area \approx _____ square <u>feet</u>

2. Color the area covered by your assigned Riemann Sum Methods using 4 equal sub-intervals.

Right-Hand= $\int_{0}^{8} Y1dx \approx$ _____sq. units, Left-Hand= $\int_{0}^{8} Y1dx \approx$ _____sq. units, and Trapezoid= $\int_{0}^{8} Y1dx \approx$ _____sq. units

Right-Hand= $\int_{0}^{8} Y1dx \approx$ _____sq. feet, Left-Hand= $\int_{0}^{8} Y1dx \approx$ _____sq. feet, and Trapezoid= $\int_{0}^{8} Y1dx \approx$ _____sq. feet

What is the significance of the 0 and 8 on the integral to this problem?______

What could be done to make this method of estimating more accurate? ______

What width would each rectangle approach if an infinite number of rectangles were "squeezed" in between 0 and 8? _____

3. Find Quartic equa	ations modeling the toenail's shape fro	om above and below of the Statue of Liberty's big toenail. Enter the
coordinates where	x-values are integers into the regressio	n feature of your calculator. Round values to the thousandth's place
Upper Curve: Y1=		Lower Curve: Y2=
(Usually I do not g	ive the values. I have students estimat	e values from the graph in order to have slightly different answers.)
x y 0 2 1 2.8 2 4.2 3 4.4 4 4.5 5 4.4 6 4.2 7 3 8 2		x y 0 1 1 6 2 8 3 9 4 -1 5 9 6 8 7 6 8 1
the x-coordinates of values for the integr	f the intersection points. The x-coording ral below.	ng the equations from step 3. Find this area by <i>integrating</i> between nate of the intersection points provide the lower, a, and upper, b,
a=	& b=	Area: $\int_{a}^{b} \left[\left(Y1 \right) - \left(Y2 \right) \right] dx \approx \underline{\qquad}$
with a reasonable es	•	er approximately <u>20</u> square feet. Use this information to come up largest toe. Then give an estimate for painting all ten toe nails.
6. Research and the	state 5 interesting facts about the Sta	tue of Liberty that you did not already know.