

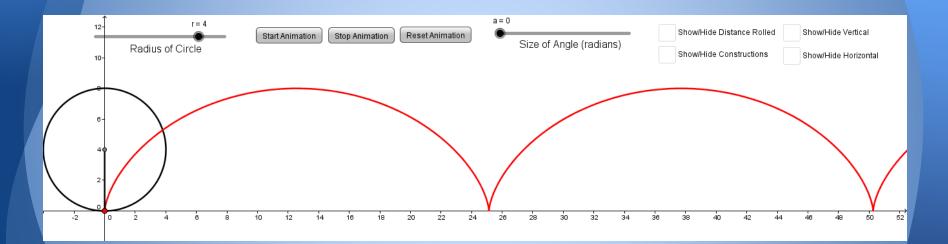
Maria Hernandez, NC School of Science and Math Taylor Gibson, NC School of Science and Math

Goals for Our Session

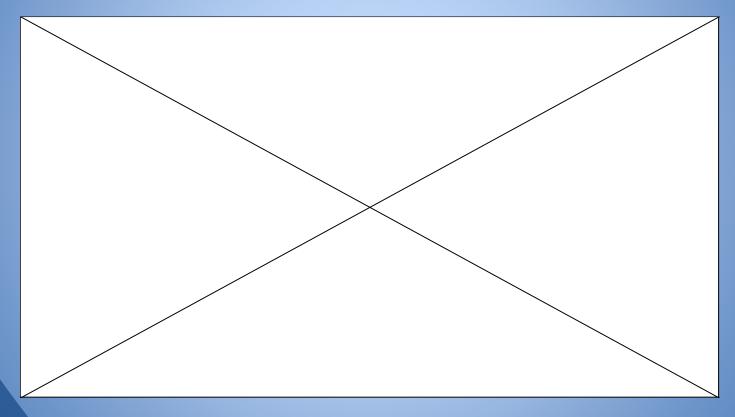
- Introduce the project and parametric equations
- Demo data collection via LoggerPro
- Create models for the collected data
- Evaluate models
- Explore the geometric representations
- Share resources to extend the project



The Cycloid



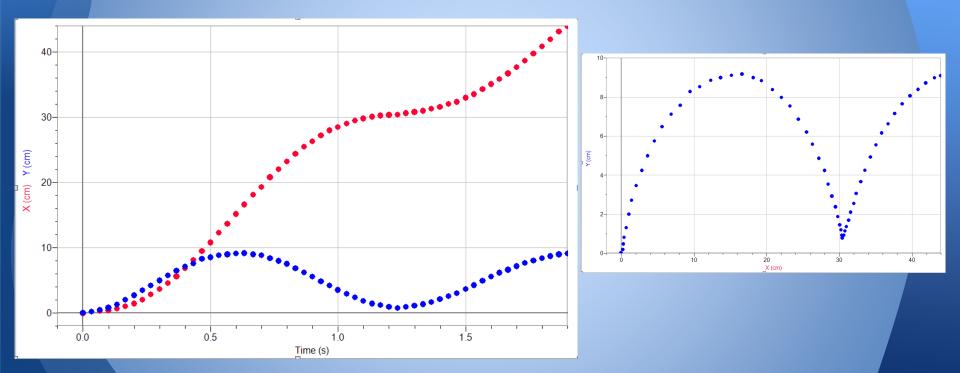
Intro to Parametric Models



Creating Models From Data

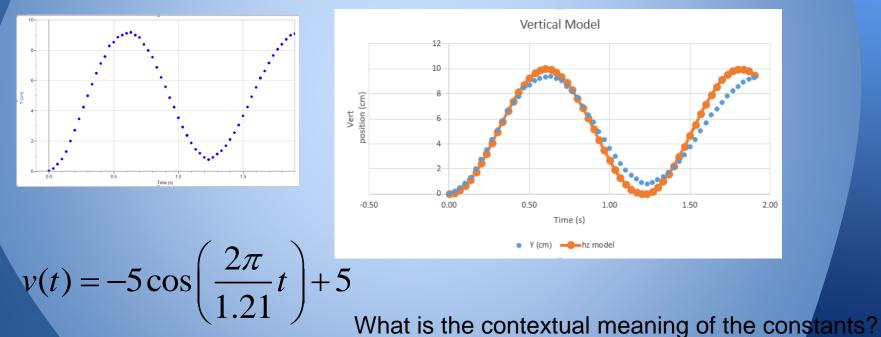
Logger Pro is a tool to capture data from a video. Our data will be shared in other forms for your use.

Data Collected from Video



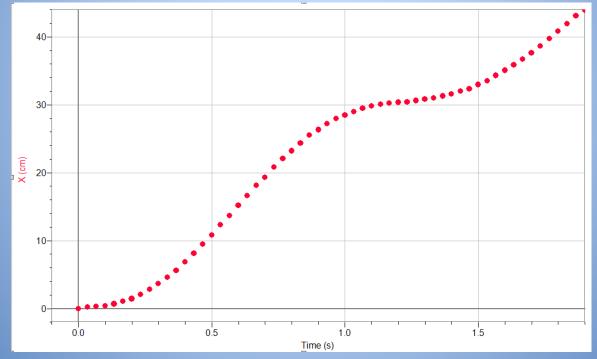
Vertical Model

Below we see the data (time, vertical position of dot)

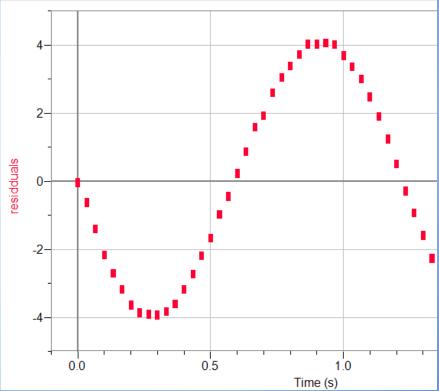


Horizontal Model

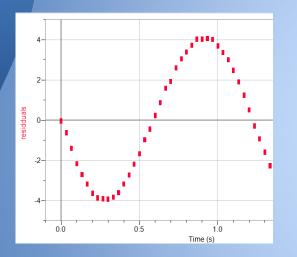
Below we see the data (time, horizontal position of dot)

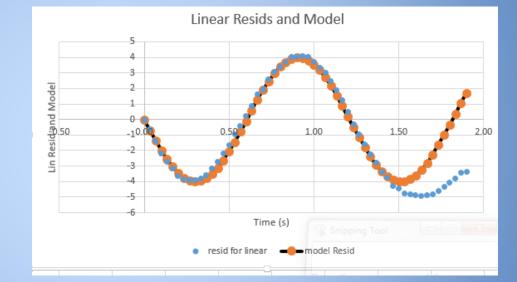


Linear Model and Residuals for Linear Model x(t) = 25.5t



Residuals for Linear Model and Model for Residuals





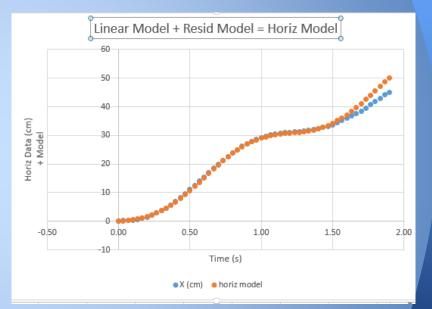
$$R(t) = -4\sin\left(\frac{2\pi}{1.21}t\right)$$

Putting the Model Together

What are some possible choices?

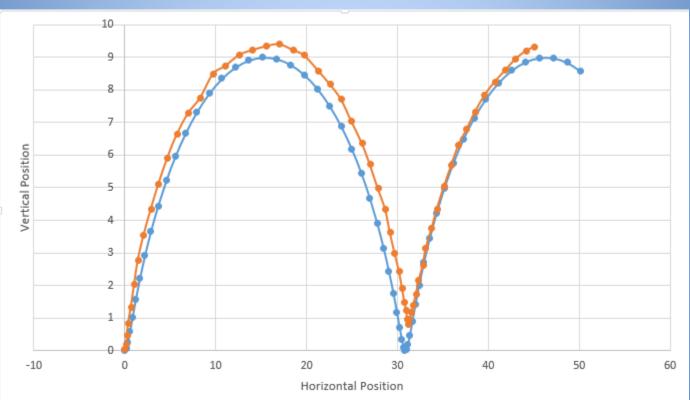
Summing the Models

$$h(t) = 25.5t - 4\sin\left(\frac{2\pi}{1.21}t\right)$$



What do the constants mean in context?

Final Model for Position of Dot

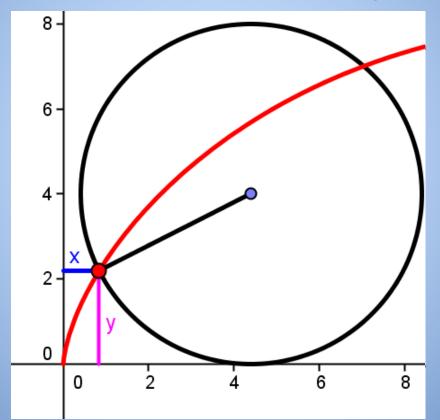


Evaluating the Models

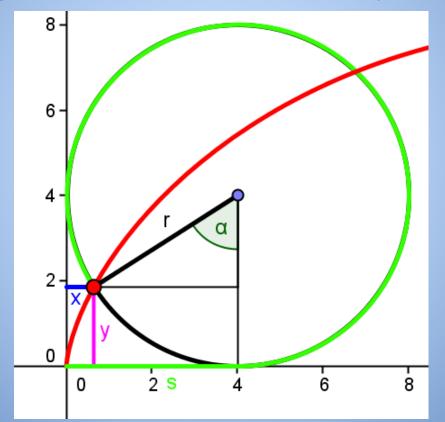
- What are the strengths and weaknesses of our models?
- How can evaluating our models help students make connections between the mathematics and the physical phenomenon?

Modeling With Geometry

Modeling with Geometry

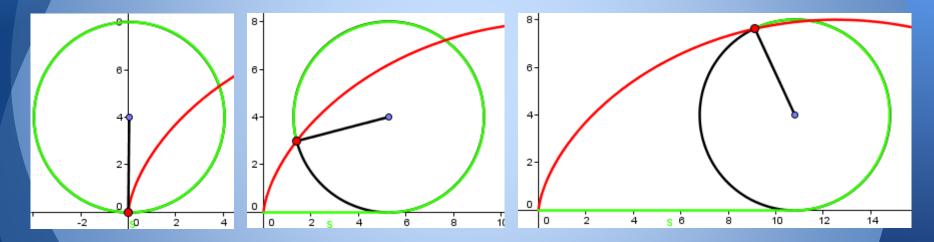


Modeling with Geometry

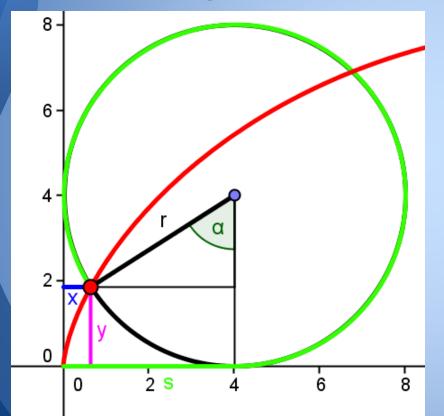


Geometric Model

Help me determine s, the distance rolled



Modeling with Geometry



Final Geometric Model

 $x(\alpha) = r\alpha - r\sin\alpha$ $y(\alpha) = r - r\cos\alpha$

Student Reflections

"One of my favorite aspects of this project was that it was (with your input and guidance when we were stuck) a self-discovery." - Thomas

"I think the coolest part of the cycloid project was that it made you think differently than normal; My first thought would have never been a combination of a cosine and linear function. I didn't even know that was a thing until this project." - Vishwa

"Hopefully, in the future, we'll be able to do a few more independent modeling investigations." -Jules

"I felt like I really wanted to learn this answer in this lab because it was something new that I got to discover by myself. Overall, the cycloid lab was very interesting and a very fun and inventive way to introduce the class into combining equations." - Matthew

Questions to Consider

Modeling Cycle - How does the project fit into a focus on math modeling?

• What's powerful about it for students?

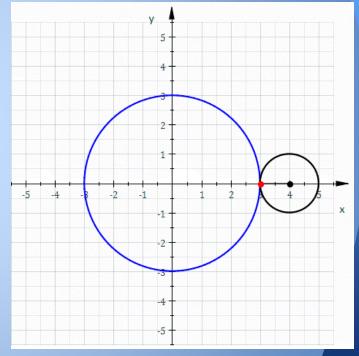
What's powerful about it for teachers?

Calculus and Geometry Extensions

- Length of path for an arch
 4·diameter
- Speed of the dot (vectors)
- Area under an arch
 - \circ 3 · (Area of circle)
- Tangent line through dot

 Passes through top of circle

 Epicycloids/Hypocycloids



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References and Resources

- NCSSM Swing Lab Materials <u>http://www.dlt.ncssm.edu/stem/content/swing-lab-documents</u>
- Cycloid Materials from This Presentation
 http://www.ncssm.edu/courses/math/cycloid/
- Inspirations Video by Cristobal Vila <u>https://www.youtube.com/watch?v=oVthC6neqVc</u>

Conferences

 Bridges Conference: Mathematics, Music, Art, Architecture and Culture Baltimore, MD July 29 - Aug 1, 2015



- 2. Anya Greer Math, Science and Technology Conference Phillips Exeter Academy, June 21 - 26, 2015
- 3. MAA/PREP Teaching Mathematical Modeling as Creating Mathematical Discovery Lincoln, NB July 20 - 25

NCSSM Teaching Contemporary Mathematics Conference

The NC School of Science and Mathematics Durham, NC, January 29 - 30, 2016 http://www.ncssm.edu/courses/math/tcm/TCM2015/



Questions?

Open Position @ NCSSM

http://www.oshr.nc.gov/jobs/

- Search Job Positions
- Departments: NCSSM

		DOCUMENTS AND LINKS				
		Search Jobs				
Search Departm	ients		Select		None	
North Carolina School of Science & Math (1)						

Thank You!

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