## Mind over Mathematics: Conveying and Cultivating a Growth Mindset

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## Agenda/Investigations

- How does mindset impact achievement?
- What role does mindset play in productive struggle?
- What does productive struggle look like in the classroom?
- What are some strategies, resources, and tools we can use to encourage the development growth mindset and productive struggle?
- Why did you become so good at it?
- How did you become so good at it?


## Famous Failures

https://youtu.be/Y6hz s2XIAU

| A. Demoted from news anchor <br> position | Oprah Winfrey |
| :--- | :---: |
| B. Cut from his high school team | Michael Jordan |
| C. Unceremoniously removed from <br> own company | Steve Jobs |
| D. Teachers said would never <br> amount to much | Albert Einstein |
| E. Fired from position for lack of <br> imagination and having no original <br> ideas | Walt Disney |
| F. Dismissed from drama school <br> with a note that read, "too shy to <br> put best foot forward" | Lucille Ball |

## The Best of the Best!

Expert - a person who has made all the mistakes that can be made in a very narrow field.

Niels Bohr
Geniuses- those who make great creative contributions, cannot be explained by talent alone, but rather by deliberate practice they devote to their field.

Ericsson, Charness, Feltovich, \& Hoffman

## Mindset Matters

- FIXED mindset teachers and students believe intelligence is fixed and it cannot be altered.
- GROWTH mindset teachers and students believe that intelligence can increase by receiving the appropriate feedback and guidance when a mistake is made.


## Mind Over Mathematics



## 50 minutes of teaching a single idea, not about math, but about the brain!

Mindsets and Math/Science Achievement. Carol Dweck. www.opportunityequation.org

## Struggle

For deeper learning to take place, struggle is not optional - it's neurologically required.

## Daniel Coyle



## Myelin: White Matter, Matters!

Firing and optimizing circuits grows myelin!

- Targeted mistake-focused practice is the best way to build a good circuit.
- Wrapping myelin around big circuits requires immense energy and time.



## Essentials of Deliberate Practice <br> (The Talent Code by Daniel Coyle)

- Deep practice (chunking)
- Ignition (inspire)
- Master Coaching 9



## Practice \& Learning

We climbed Mount Everest on a Tuesday morning.

Gn inromya Dseut Anotser ev e Tnuomde bmilcew.


## Productive Struggle

> Productive Persistence = Tenacity + Good Strategies

The effort to make sense of something, to figure something out that is not immediately apparent.
Hiebert \& Grouws, 2007

Opportunities for delving more deeply into understanding the mathematical structure of problems and relationships among mathematical ideas, instead of simply seeking correct solutions.

NCTM, Principles to Actions

Effortful practice that goes beyond passive reading, listening, or watching - that builds useful, lasting understanding and skill.

## Productive Struggle

## What are some behaviors that productive strugglers exhibit in the classroom?



## Powerful Practices: <br> Fostering Growth Mindset \& Productive Struggle

## The teacher:

- creates a climate that supports mathematical thinking and communication
- responds in a way that keeps the focus on thinking and reasoning rather than only getting the right answer

Process vs Person
Praise: Instead of
praising students for their talent or smarts, teachers should praise students for:

- The strategies they use
- The specific work they do
- Their persistence or effort


## The students are:

- accustomed to explaining their ideas and questioning solutions that don't make sense to them
- not afraid to take risks and know that it is acceptable to struggle with some ideas and to make mistakes
- recognize that mistakes are a means to learning and not an end

| Mindset Analysis Questionnaire: Read each statement and check the column that best describes you. (Answer as your students would!) |  | ※ |  |  |
| :---: | :---: | :---: | :---: | :---: |
| 1. You are either good at math or you aren't and you can't change it. |  |  |  |  |
| 2. You can only do well in math if you are clever. |  |  |  |  |
| 3. Your memory affects how good you are in math. |  |  |  |  |
| 4. Learning new mathematical skills does not mean you are changing your ability. |  |  |  |  |
| 5. You can do a lot to change how clever you are. |  |  |  |  |
| 6. You can do a lot to change how well you understand mathematics. |  |  |  |  |
| 7. If you can answer a question quickly you are good at math. |  |  |  |  |
| 8. How many answers you get right on a test shows how good you are at math. |  |  |  |  |
| 9. Practice exercises are the best way to learn new mathematical skills. |  |  |  |  |
| 10. Watching a teacher do examples is the best way to learn new mathematical skills. |  |  |  |  |
| 11. Trying a problem you don't know how to solve is the best way to learn new mathematical skills. |  |  |  |  |
| 12. The class you are in tells you how good you are at math. |  |  |  |  |
| 13. I prefer to work on questions that challenge me rather than questions that I find easy. |  |  |  |  |

## Autobiography

Carol Dweck says that all the world's parenting advice can be distilled to two simple rules: pay attention to what your children are fascinated by, and praise them for their effort.

What are your students fascinated with?

## Mathematical Tasks

There is no decision a teacher makes that has a greater impact on students' opportunities to learn and on their perceptions about what mathematics is than the selection or creation of the tasks with which they engage students in studying
mathematics (Lappan and Briars, 1995).

## Problem Solving

 StrategiesAllowing students to approach solving problems in different ways using different strategies helps them to better understand mathematics, develop mathematical fluency, and see mathematics as worthwhile and doable. Doing so sets the stage for transferring conceptual knowledge to new situations (Many, Fyfe, Lewis, \& Mitchell, 1996).

## Mathematical Tools

Effective teachers know that using a variety of mathematical tools shapes the way that students think and helps build conceptual understanding of the hows and whys of mathematics (Fuson et. Al. 1992)

## What's the pattern/order to these numbers???

# $8,5,4,9,1,7,6,3,2,0$ 

> Eight, Five, Four
> Nine, One, Seven
> Six, Three, Two, Zero

## Cartoon Critters



Each of the Critters wants their own space. Can you draw two quadrilaterals around the critters to give them each their own separate space?

# Multiplication Table Code Breaker What number does each letter represent? 

$$
\begin{array}{rrrrr}
A & E & C & D & J \\
\times F & \frac{x F}{} & \frac{x F}{G C} & \frac{x F}{A B} & \frac{x F}{H J} \\
\hline G J & & & & \\
G & G B & F & H & K \\
\frac{x F}{} & \frac{x F}{F B} & \frac{x F}{A F} & \frac{x F}{C H} & \frac{x F}{H C}
\end{array}
$$

This is the multiplication table from $1 \times 1$ to $9 \times 9$.
The rows are in the wrong order and so are the columns. Each letter stands for one of the digits $0,1,2,3,4,5,6,7,8,9$.

Can you crack the code?

| $x$ | $X$ | $R$ | $S$ | $T$ | $Q$ | $Z$ | $V$ | $W$ | $Y$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $Z$ | $R$ | $T Y$ | $T U$ | $Z$ | $T R$ | $X$ | $Y$ | $T X$ | $T Z$ |
| $\mathbf{W}$ | $Z R$ | $S Y$ | $V S$ | $W$ | $Y V$ | $T X$ | $Z T$ | $X Q$ | $X Z$ |

$Y \quad Z X \times R$ VU $Y$ XX TX TR $X Z V Y$ $X$ TY VZ $Z U X V Y R \quad T Z \quad Z R Z X$ $V$ TX IX TS $V$ LW $Y$ Q $Z T$ TR
$T \quad X \quad R \quad S \quad T \quad Q \quad Z \quad V \quad W \quad Y$
$R \quad V Z Y X X U R \quad W Z$ TY XX TY YR
$S$ LU XU ZS $S$ XS TU TS VS VV
Q VY WZ XS Q RT TR KW VV IX

## Mathematical Tools

Just a rectangle to...

- engage learners
- promote mathematical thinking
- foster problem solving and reasoning
- Assess knowledge and understanding


## Folding with Finesse!!!

Make one
fold to make:
Make one fold to make:

2 trapezoids

Make one fold to make:

1 triangle \&
1 pentagon

## Effective Questioning

## POWERFUL K - 12 Generic Response Questions

- How did you work that out?
- Could you solve that another way?
- Can you summarize and/or generalize your result(s)?

Source: NCTM Professional Development Guidebook for Prospective on Teaching Mathematics

# Closed Questions... 

VS
Open Questions...


## What is the mean of 5 , $11,7, \& 1$ ?

## What about this

 problem makes it limiting and closed?How can we make it more open?


## Questions for Supporting the Development of the CCSS Mathematical Practices

| How is this task similar to a previous task you have completed? <br> How might you solve a simpler task to help with this? <br> What helped you to be successful in solving the problem? | MP1. Make sense of <br> problems and persevere in <br> solving them. |
| :--- | :--- |
| What is the relationship between the data/situation and the equation? <br> How are these answers alike? Different? <br> Can you think of an example that would fit this expression? | MP2. Reason abstractly and <br> quantitatively. |
| Why did you use [a graph] to solve it? <br> How did you get [that equation]? <br> What do the rest of you think about Raul's strategy? <br> Are these strategies different or alike? | MP3. Construct viable <br> arguments and critique the <br> resonating of others. |
| How does your model (equation) connect to the situation? <br> Where can you find [the rate] in this situation? The table? The equation? <br> Are these two equations equivalent? Which (if any) is more efficient? | MP4. Model with <br> mathematics. |
| How might a number line help you think about it? <br> What manipulative or picture might you use? | MP5. Use appropriate tools <br> strategically. |
| Can you elaborate on your explanation? <br> Can you explain what each variable represents? | MP6. Attend to precision. |
| Does this problem remind you of another problem you have solved? <br> What patterns did you notice across these problems? | MP7. Look for and make use <br> of structure. |
| What patterns do you notice across these problems? <br> How are these problems the same? Different? | MP8. Look for and express <br> regularity in repeated <br> reasoning. |

Source: Maggie B. McGatha \& Jennifer M. Bay-Williams
$S=$ Student Expectation $T=$ Teacher Action $P=$ Productive Struggle Success Indicator (Source: NCTM Principles to Actions)

| Communicating about one's <br> thinking during a task <br> makes it possible for others <br> to help that person make <br> progress on the task. | Students are able to use <br> tools to solve tasks that <br> they cannot solve without <br> them. | Ask students to explain and <br> justify how they solved a <br> task. Value the quality of <br> the explanation as much as <br> the final solution. |
| :--- | :--- | :--- |
| Give students access to <br> tools that will support their <br> thinking processes. | Ask students to explain <br> their thinking and pose <br> questions that are based on <br> students' reasoning, rather <br> than on the way that the <br> teacher is thinking about <br> the task. | Students explain how they <br> solved a task and provide <br> mathematical justifications <br> for their reasoning. |
| Correct solutions are <br> important, but so is being <br> able to explain and discuss <br> how one thought about and <br> solved particular tasks. | Diagrams, sketches, and <br> hands-on materials are <br> important tools to use in <br> making sense of tasks. | Students explain their <br> thinking about a task to <br> their peers and the teacher. <br> The teacher asks probing |
| question based on the |  |  |
| student's thinking. |  |  |

$\mathbf{S}=$ Student Expectation $\mathbf{T}=$ Teacher Action $\mathbf{P}=$ Productive Struggle Success Indicator NCTM, Principles to Actions

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| student's thinking. |  |  |$\quad$| l S |
| :--- |

## Teachers are "Identity Builders" Robert Q. Berry, III

- You inspire and
 motivate students
- You arm students with multiple plays
- You transform students' mistakes into opportunities to learn and develop skills


## Resources

- Growth Mindset
http://www.edutopia.org/blog/growth-mindset-common-core-math-cindy-bryant
- Productive Struggle http://web.learnbop.net/blog/two-types-of-struggle-in-problem-solving-
- Mathematical Habits of Mind http://www.edutopia.org/blog/mathematical-habits-of- mind-cindybryant
- Creative Problem Solving in School Mathematics ISBN: 0-395-34546-4
- LearnBop Efficacy Study Report http://go.learnbop.com/efficacy-study-results-full-report
- www.learnbop.com BOOTH 431


## QUESTIONS???

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