

Welcome

Ensuring Mathematical Success for All

Multi-Tiered Systems of Support: Interventions and Assessment Strategies

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NATIONAL COUNCIL OF
TEACHERS OF MATHEMATICS

Topics for Today

- Brief overview of **RtI Model**, one version of a multi-tiered system of support (**MTSS**)
- What helps students with disabilities build **cognitive structures** and **connections** in mathematics?
- Research based **Interventions** to try (not buy)
- **Diagnostic interviews** - a way to gather feedback on **students' mathematical thinking**
- **Strategies** for teaching math that **DON'T EXPIRE!!**

Foundational Questions

Content – what comes before the Common Core State Standards for Mathematics at your grade level?

What are the foundational ideas in mathematics that students can build on? (not dead ends)

How do you teach these foundational concepts to students who struggle?

Why aren't Tier 2 Interventions Helping?

- Recent studies reveal that teachers providing Tier 2 mathematics interventions to elementary and middle grade students largely used **worksheets** (Foegen & Dougherty, 2010; Swanson, Solis, Ciullo & McKenna, 2012)
- In my travels to classrooms and schools many use a **one-size-fits-all generic computer program** (a worksheet on a computer).

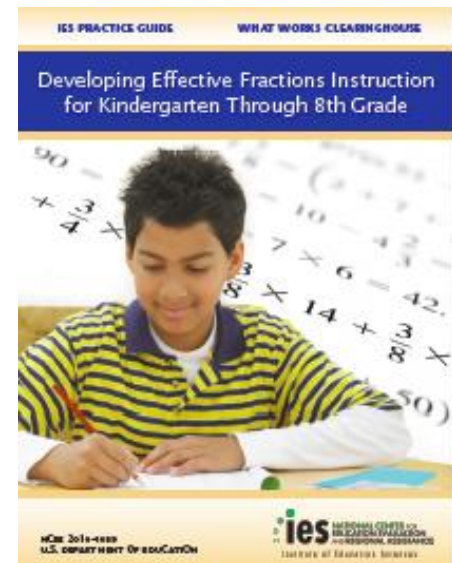
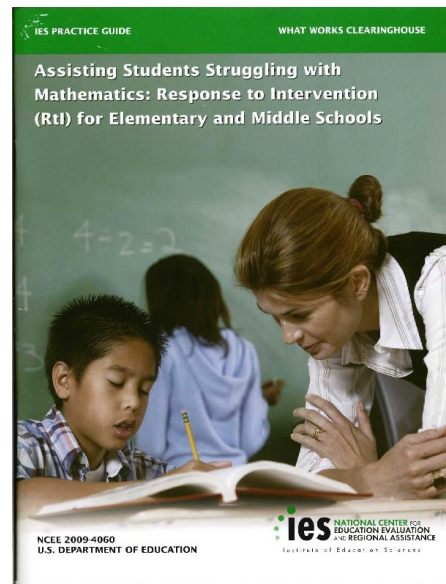
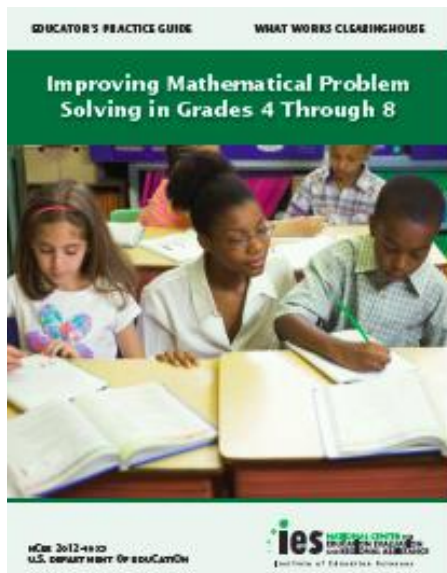
Worksheets + computer programs \neq understanding

What might a student's brain look like?

What if one student had a good understanding of a mathematical concept and the other student had just memorized it (or lacked the ability to memorize – like a student with disabilities)?

Recommendations for supporting students struggling in mathematics

- Recommendations are based on **strong** and **moderate** levels of evidence resulting from comprehensive reviews of current research



Gersten, R., Beckmann, S., Clarke, B., Foegen, A., Marsh, L., Star, J. R., & Witzel, B. (2009). *Assisting students struggling with mathematics: Response to Intervention (Rti) for elementary and middle schools (NCEE 2009-4060)*. Washington, DC: National Center for Education Evaluation and Regional Assistance, Institute of Education Sciences, U.S. Department of Education. Retrieved from <http://ies.ed.gov/ncee/wwc/publications/practiceguides/>.

Intervention Recommendations from Research

- **Concrete--Semi-Concrete--Abstract (CSA)** approach
- Explicit instruction
- Underlying mathematical structures
- Examples (and counterexamples)
- Feedback – Not teacher to student but students' feedback to teacher on what they know and don't know

Newman-Gonchar, R., Clarke, B., & Gersten, R. (2009). A summary of nine key studies: Multi-tier intervention and response to interventions for students struggling in mathematics. Portsmouth, NH: RMC Research Corporation, Center on Instruction.

Hattie, J. (2009). *Visible learning: A synthesis of over 800 meta-analyses relating to achievement*. New York: Routledge.



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So, What did you learn in school?

- With the person sitting next to or around you, decide if the rules shown are always true.
- If it is not always true, find a counterexample.
- Addition and multiplication make numbers bigger.
- When you multiply by 10, just put a 0 on the end of the number.
- The longer the number, the larger the number.

Addition and multiplication make “bigger”

$$32 + 67 = 99$$

$$15 \times 10 = 150$$

$$-3 + (-14) = -17$$

$$\frac{1}{3} \times \frac{2}{7} = \frac{2}{21}$$

$$15 + 0 = 15$$

When you multiply by 10, just put a 0 on the end of the number.

$$15 \times 10 = 150$$

$$4.5 \times 10 = 45.0$$

$$4.5 \times 10 \neq 4.50$$

The longer the number, the larger the number.

$$1,278,931 > 1,469$$

$$1.3 > 1.0118743$$

$$1.02 < 1.2$$

Impact of Rules

- Students use rules as they have interpreted them.
- They often do not think about the rule beyond its application.
- When even the best students find that a rule doesn't work, it is unnerving and scary.

Goal – Try to AVOID DEAD ENDS

“13 Rules that Expire” (Karp, Bush & Dougherty August 2014 in *Teaching Children Mathematics*) TCM article of the YEAR!

What do we know?

- Telling isn't teaching.
- Told isn't taught.
- Explicit instruction isn't telling.

So, Karp

What's an example of your so called - explicit teaching based on structure, examples, concrete, semi-concrete, abstract understanding that is not "telling" and will reach my many students who are struggling bringing them to higher levels of mathematical understanding through the creation of blue lines?

Let's start with Word Problems

At all grades students who struggle see each problem as a **separate endeavor**

They **focus on steps** to follow rather than the behavior of the operations

They tend to use **trial and error** – (disconnected thinking – not relational thinking)

They need to focus on **actions, representations** and **general properties of the operations**

CCSSM Appendix – Common Addition and Subtraction Situations

	Result Unknown	Change Unknown	Start Unknown
Add to	Two bunnies sat on the grass. Three more bunnies hopped there. How many bunnies are on the grass now? $2 + 3 = ?$	Two bunnies were sitting on the grass. Some more bunnies hopped there. Then there were five bunnies. How many bunnies hopped over to the first two? $2 + ? = 5$	Some bunnies were sitting on the grass. Three more bunnies hopped there. Then there were five bunnies. How many bunnies were on the grass before? $? + 3 = 5$
Take from	Five apples were on the table. I ate two apples. How many apples are on the table now? $5 - 2 = ?$	Five apples were on the table. I ate some apples. Then there were three apples. How many apples did I eat? $5 - ? = 3$	Some apples were on the table. I ate two apples. Then there were three apples. How many apples were on the table before? $? - 2 = 3$
Put Together/ Take Apart ²	Total Unknown	Addend Unknown	Both Addends Unknown ¹
	Three red apples and two green apples are on the table. How many apples are on the table? $3 + 2 = ?$	Five apples are on the table. Three are red and the rest are green. How many apples are green? $3 + ? = 5, 5 - 3 = ?$	Grandma has five flowers. How many can she put in her red vase and how many in her blue vase? $5 = 0 + 5, 5 = 5 + 0$ $5 = 1 + 4, 5 = 4 + 1$ $5 = 2 + 3, 5 = 3 + 2$

Warm up task

- Using a number family like 9, 6, 15, create an addition or subtraction story problem that you would have students in your classroom solve.

Creating Mental Residue

- Establishing foundational understanding
- Modeling the physical action is the important part and doesn't go away
- Acting and “doing” the process supports students' thinking about the operation

Dougherty, B. J. (2008). Measure up: A quantitative view of early algebra. In Kaput, J. J., Carraher, D. W., & Blanton, M. L. (Eds.), *Algebra in the early grades*, (pp. 389–412). Mahwah, NJ: Erlbaum.

Some people will say...

I think this approach will
confuse my students!



The Infamous Shepherd Problem

:

There are 25 sheep and 5 dogs in a flock. How old is the shepherd?

Other options?

Would your students be able to discern which of the following three options would be the correct answer?

- The shepherd is 30 years old
- The shepherd is 125 years old; and
- It is not possible to tell the shepherd's age from the information given in the problem.

Danger - Key Words ahead

Mark has 3 packages of pencils. There are 6 pencils in each package. How many pencils does he have in all?

9

Explicit instruction - structure of word problems

The Myth of Keywords

- Keywords do not—
 - Develop of sense making or support making meaning
 - Build structures for more advanced learning
 - Appear in many problems
- Students consistently use key words inappropriately
- Multi-step problems are impossible to solve with key words (and two step problems start in 2nd grade)

Which number sentences would students say are True? False?

$$7 = 7$$

$$2 + 5 = 4 + 3$$

$$5 + 1 = 7$$

$$7 = 2 + 5$$

- Which equations would confuse them?

Diagnostic Interviews for Progress Monitoring

Give a task - collect students' mental strategies

No instruction – just ask questions

Capture student feedback on their thinking

Let students use tools for demonstrating
reasoning

$$8 + 4 = \boxed{12} + 5$$

Use information gathered to improve instruction

Try These on the Balance

- Move one weight from each side of the balance to a new peg, can you maintain the equality? How?
- $3 \times 4 = 12$
- $2x + 3 = 17$ How can you show this on the balance?

Equal Sign - Two Levels of Understanding

Operational - students mistakenly see the equal sign as signaling something they must “do” with the numbers such as “give me the answer.”

Relational - students use the relationships between the two quantities to balance the sides of the equation.

- Do students use relational thinking to generalize rather than actually computing the individual amounts.?
- Do they see the equal sign as relating to “greater than,” “less than,” and “not equal to.”

What is the long term danger?

- If middle grades students think the equal sign means “put the answer next,” what happens when they move to algebraic equations such as $3x = 2x + 3$?

Common Core State Standards

Grade 1:

Understand the meaning of the equal sign, and determine if equations involving addition and subtraction are true or false. *For example, which of the following equations are true and which are false? $6 = 6$, $7 = 8 - 1$, $5 + 2 = 2 + 5$, $4 + 1 = 5 + 2$.*

Let's go back to Tier 1 Core Instruction

Headline – *New York Times*

July 27, 2014

(New Math) – (New Teaching) = Failure

Why do Americans Stink at Math - Green

What were the Main Points?

- Common Core State Standards – Fosters intuitive thinking through real-world examples – that **is** the best way to teach mathematics
- Real Problem – Teachers are being asked to teach in ways they've not experienced as students – or have not been effectively taught
- America invented the best ways of teaching math as espoused by NCTM and supporting research – yet not enough teachers are using these methods

What is the Whole School Agreement?

- Decide on the language and models everyone will use – be precise and consistent
- Prepare all students, from the beginning to walk out of the building
- Think about the level of teaching – are challenging students at the highest level?
- Get kids “doing mathematics” so they can build mental residue and long lasting understanding

Shifts in Thinking

- **Teacher talking and doing TO students talking and doing – never say anything a kid can say**
- **Using key words TO building student understanding with reasoning and sense making**
- **Learning disconnected rules and algorithms TO engaging students in productive struggle with rich, high-quality problems**

An Article coming soon – to a TCM
journal near you!!!

The Whole School Agreement

Karp, Bush & Dougherty – In press
in **Teaching Children Mathematics**