

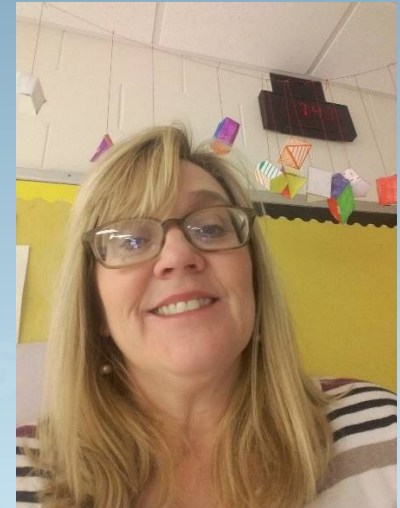
Explore Absolute Value

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TEACHERS OF MATHEMATICS

The Vision of the CRC

Create an online mathematics education professional learning community that is the go-to site for teachers.



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ARCs

- Activities with Rigor and Coherence
- Sequence of 2–4 lessons that...
 - support Principles to Actions
 - addresses a specific math topic
 - scaffolds effective teaching
 - supports the 8 SMPs
 - demonstrates the 5 Practices for Orchestrating Productive Mathematics Discussions
 - integrates the wide array of NCTM resources



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ARC Topics

- Illumination activities
 - Law of Sines and Cosines
 - Coding and Decoding
- New topics
 - Absolute Value
 - Triangle Congruence via Transformations
 - Barbie Bungee - Regressions
 - Graphing Trigonometric Functions
 - Ferris Wheel: Graphs of Sine and Cosine Functions



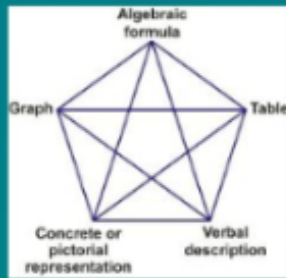
Absolute Value

- What do you think of when you hear absolute value



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ABSOLUTE VALUE



#1 Distance

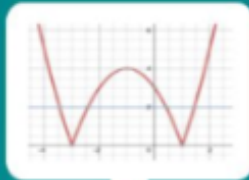
#2 Reflection

#3 Equation

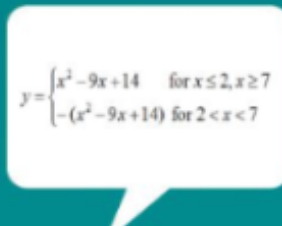
MULTIPLE REPRESENTATIONS



Number Line



Coordinate Plane



Piecewise Function

What does ABSOLUTE VALUE mean?



What does absolute value mean?

Absolute Value on the Number Line

Double Number Line

What could the function be? Make a prediction.

$$f(x) =$$

$$f(-3) =$$

Absolute Value on the Coordinate Plane

- What is the relationship between a function and its' absolute value?
- What do you notice? What do you wonder?
- Graph by hand, TI calculators, Desmos, a combination of those, etc.

Absolute Value on the Coordinate Plane

- What were some of the functions you chose for problems 7 & 8?
- Rewrite each absolute value function as a piecewise defined function.
- [Desmos](#)

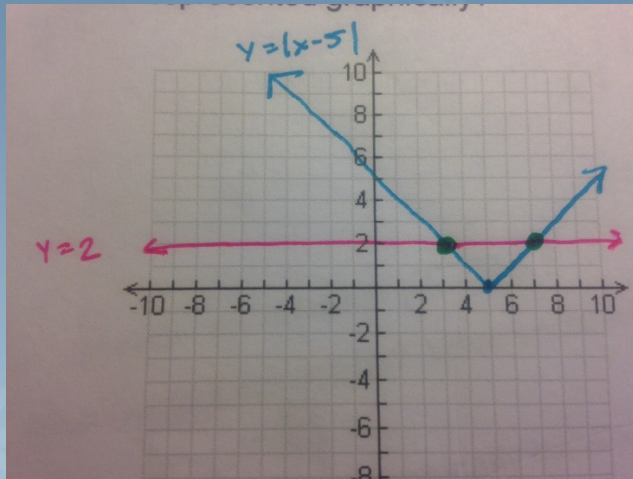
Absolute Value on the Coordinate Plane

- How does reflection help us understand the graph of linear and non-linear absolute value functions? What type of assessment might address this question?

Solving Absolute Value Equations

- How is a solution to a system of equations represented graphically.

Solving Absolute Value Equations



Solution(s): 3, 7

Solve the equation algebraically by rewriting the absolute value function as a piecewise function.

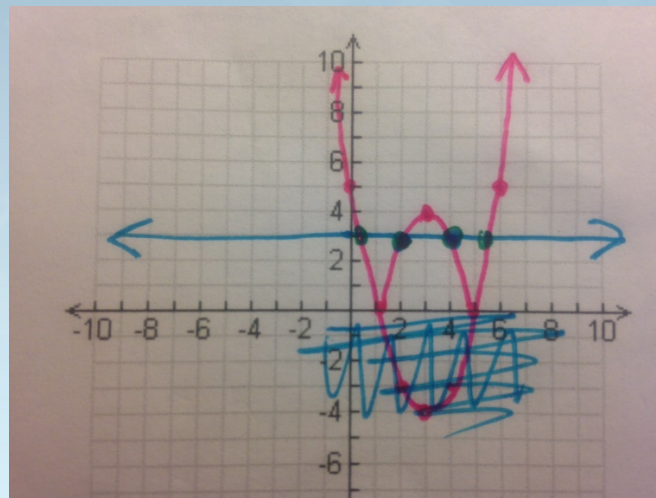
$$y = \begin{cases} x - 5 & x \geq 5 \\ -(x - 5) & x < 5 \end{cases}$$

$$x - 5 = 2 \qquad \qquad \qquad -(x - 5) = 2$$

$$x = 7 \qquad \qquad \qquad x - 5 = -2$$

$$\qquad \qquad \qquad \qquad \qquad \qquad x = 3$$

4
= 3



Solution(s): 4, 2, 3 ± √7

Solve the equation algebraically by rewriting the absolute value function as a piecewise function.

$$y = \begin{cases} (x - 3)^2 - 4 & x \geq 5, x \leq 1 \\ -(x - 3)^2 + 4 & 1 \leq x \leq 5 \end{cases}$$

$$(x - 3)^2 - 4 = 3 \qquad \qquad \qquad -(x - 3)^2 + 4 = 3$$

$$(x - 3)^2 = 7 \qquad \qquad \qquad -(x - 3)^2 = -1$$

$$x - 3 = \pm\sqrt{7} \qquad \qquad \qquad (x - 3)^2 = 1$$

$$x = 3 \pm \sqrt{7} \qquad \qquad \qquad x - 3 = 1 \quad x - 3 = -1$$

$$\qquad \qquad \qquad \qquad \qquad \qquad x = 4 \qquad \qquad \qquad x = 2$$

Solving Absolute Value Equations

Solve the equation graphically by rewriting the equation as a piecewise function.

Solution(s): $\frac{9 \pm \sqrt{13}}{2}$

Solve the equation algebraically by rewriting the absolute value function as a piecewise function.

$$x^2 - 9x + 14 = 3 \quad - (x^2 - 9x + 14) = 3$$

$$x^2 - 9x + 11 = 0 \quad x^2 - 9x + 17 = -3$$

$$x = \frac{9 \pm \sqrt{81 - 4(1)(11)}}{2} \quad x = \frac{9 \pm \sqrt{81 - 4(1)(17)}}{2}$$

$$= \frac{9 \pm \sqrt{57}}{2} \quad = \frac{9 \pm \sqrt{13}}{2}$$

$$\approx 7.5, 1.5 \quad x = 6.3, 2.7$$

Could a non-solution be? Explain.

Solve the equation algebraically by rewriting the absolute value function as a piecewise function.

$$\sqrt[3]{x-4} = 2 \quad -\sqrt[3]{x-4} = 2$$

$$x-4 = 8 \quad \sqrt[3]{x-4} = -2$$

$$x = 12 \quad x-4 = -8$$

$$x = -4$$

absolute value equations by graphing compared to

WANT MORE?

- Session 194: Explore Absolute Value & Contribute to the Development of NCTM's ARCs (8-10)
- Session 220: Explore Real-World Statistics, Simulate a Bungee Jump & Meet NCTM's ARCs. (10-12)
- Session 276: Explore Growing Patterns & Engage with Manipulatives with NCTM's ARCs (3-5)
- Session 336: Explore Area Concepts & Contribute to the Development of NCTM's ARCs (6-8)
- Session 591: Explore Counting Strategies with NCTM's Activities with Rigor & Coherence (Pk-2)



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See: www.nctm.org/ARCs/

Get Involved!

Add your comments!

- modifications
- general thoughts
- opportunities for differentiation
- reflection after implementation

Contribute...

- future ARCs
- great projects that have worked for you

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<http://www.nctm.org/ARCs/>