## Describing Patterns Algebraically: Find the Next or Find the Nth?

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204 C (Pennsylvania Convention Center)

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"How do you see this figure growing?" is a simple yet engaging question for the study of patterns and relationships. We'll look at the distinction between describing the next figure in a pattern and the nth figure in a pattern, and how this distinction impacts students' work with proportional relationships, slope, and functions.

## Which one doesn't belong?

(Check out more at http://wodb.ca/ and @WODBMath; and at http://www.visualpatterns.org/)


## How do you see this pattern growing?



Figure 1
Figure 2
Figure 3
Figure 4

| Sketch the 10th figure. | Sketch the 27 figure. |
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| If you know what Figure 12 looks like, what <br> would you do to draw the next figure? | How would you figure out how many X's are <br> in the 100th figure? |

## Student work for this pattern:

|  |  | $X$ |
| :--- | :--- | :--- |
| $X$ | $X$ | $X$ |
| $X$ | $X$ | $X$ |
| $X X X X$ | $X$ | $X$ |
| $X X X X X X X X$ |  |  |

Figure 1
Figure 2
Figure 3

| $\begin{aligned} & \mathrm{X} \\ & \mathrm{X} \\ & \mathrm{X} \times \mathrm{XX} \end{aligned}$ | $x$ <br> X <br> X <br> XXXXX | $\begin{aligned} & x \\ & x \\ & x \\ & x \\ & x \\ & x \times x \times x \end{aligned}$ |  |
| :---: | :---: | :---: | :---: |
| Figure 1 | Figure 2 | Figure 3 |  |
| Fiqure $=x$ | $x=y$ | $y+2$ | $x$ $y$ <br> 1 6 <br> 2 8 <br> 3 10 <br> 4 12 |



## What's the same? What's different?



| $\begin{aligned} & x \\ & x \\ & x \times x>x \end{aligned}$ | $\begin{aligned} & \infty \\ & x \\ & x \\ & x \times x=8 \end{aligned}$ | $\begin{aligned} & (x) \\ & x \\ & x \\ & x \\ & x \\ & x \times x \times x \end{aligned}$ |
| :---: | :---: | :---: |
| Figure 1 | Figure 2 | Figure 3 |
|  | $(n+3)+(n+1)$ |  |

## Practical Tips

- Don't discourage recursive thinking. It's the entry point!
- Do lot's of drawing!
- Draw the next and draw the 27th
- What's changing and what's not?
- Teach them how to organize their thinking when they become disorganized.
- Look for and describe the connections
- Between recursive rule and functional rule
- Between different forms of the functional rule
- Do these often!

