## Raisins, Ropes, and a Whole Lot More: Six Activities to Open the Door!

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## Warm-Up Door

In this 4-by-4 grid, your task is to create a continuous sequence of positive integers, 1 through 16, using the values already in place and making only vertical and horizontal moves.


## Warm-Up Door:

## Where Could 7 Go?

In this 5-by-5 grid, your task is to create a continuous sequence of positive integers, 1 through 25, using the values already in place and making only vertical and horizontal moves.

| 5 |  |  | 24 |  |
| :--- | :--- | :--- | :--- | :--- |
|  |  |  |  | 20 |
|  |  |  |  |  |
|  | 9 | 16 |  | 14 |
|  |  |  |  |  |

## Warm-Up Door: What's Your Third Move?

| $2 \div$ |  | $2-$ |  |
| :--- | :--- | :--- | :--- |
| 2 | $1-$ |  | $6 \times$ |
| $5+$ |  |  |  |
| $4+$ |  | $2-$ |  |

## Door \#ı: Guess My Age

President Obama ..... 55
Hillary Clinton ..... 69
LeBron James ..... 31
Killer Mike ..... 41
Bernie Sanders ..... 75
Martina Navratilova ..... 60
Julia Roberts ..... 49
Danica Patrick ..... 34
John Glenn ..... 95
Sarah Palin ..... 52
Donald Trump ..... 70
Britney Spears ..... 34

Guess the Age!


Guess the Age!


## Door \#2: All Knotted Up

1) Grab a rope. Measure and record its length in cm .
2) Tie a knot into the rope.
3) Measure the length of the rope, end to end, to the nearest half cm and record that length in the table below.
4) Repeat this until you have 10 knots in the rope. Make every attempt possible to duplicate the original knot (size, tightness) with every additional knot you create.
5) Collect rope-length data for 0 to 10 knots from another group.
6) Graph your results.

| Number <br> of Knots | Length of <br> Your Rope | Length of <br> Other Group's Rope |
| :---: | :---: | :---: |
| 0 |  |  |
| 1 |  |  |
| 2 |  |  |
| 3 |  |  |
| 4 |  |  |
| 5 |  |  |
| 6 |  |  |
| 7 |  |  |
| 8 |  |  |
| 9 |  |  |
| 10 |  |  |

a) Write a sentence or two to describe the relationship between the number of knots and the length of the rope.
b) Generate an equation to represent the relationship between the number of knots and the length of the rope.
c) Use your equation to predict the length of your rope after tying 15 knots.
d) Use your equation to predict the number of knots that would be on your rope if your rope were 24 cm long.

## Door \#3: Is That Unusual?

$\square$ Suppose the Kick-a-Poo Milling Company made this claim about their Raisin Bran:

$$
\begin{aligned}
& \text { In our } 20 \text {-ounce box of raisin bran, } \\
& \text { we average } 143 \text { raisins per box. }
\end{aligned}
$$

$\square$ Now suppose you just opened a 20-ounce box of Kick-a-Poo Raisin Bran and accurately counted 174 raisins. Would this number of raisins be a rare occurrence? Would it seem unusual to you? Write a sentence to explain your response.

## Door \#4: How Much Cement?

A landscape engineer is adding a concrete patio to a home as part of a landscaping project. Her crew uses thin flexible strips of wood as a border for the wedge-shaped patio. One strip of wood measures 16 feet long and is bent in the arc of a circle so its ends are 12 feet apart. Concrete will fill the wedge created by the arc of the circle and two radii, as shown here. The concrete will be 4" thick.

How long is the radius of this wedge-shaped patio? How many cubic yards of concrete must be ordered for the patio?


## Door \#5: Deice a Fuel Line

$\square$ While living and working in Norway I drove a 1967 Volkswagen Beetle. As cold temperatures approached, the mechanic at a local garage suggested I use a gasoline additive to absorb any moisture that might condense in the fuel line of the Beetle. I dutifully purchased the product, generically referred to as deicer, and poured it in with the gasoline when I next filled the tank.

- The information on the deicer label suggested regular use during cold temperatures and recommended adding a can with every fuel fill. I made a mental note to do that, but at the same time I began to wonder:

What happens in that fuel tank as I add more and more deicer?
Won't the tank eventually be filled with just deicer?

## Door \#6: A Typical Slice

## Bonus Door A: Viewing Tubes

Most of us at one time or another have used a cardboard or plastic tube as a telescope. Although the tube does not actually enlarge what we see, it does help us focus on a narrow field of vision.

In this activity, we are going to try to understand and predict how much of a scene is visible through a viewing tube at a distance.
Your group should have a viewing tube and a measuring tape.

## Bonus Door A: Viewing Tubes

1. First, try to identify all the variables that you think might effect how much of a vertical wall is visible through a viewing tube. These may be properties of what you're looking at (e.g., how far away is it), or properties of the particular tube that you're using.
2. Next, gather data with your particular tube. Since you are using one particular tube, some of your variables will be fixed. See if you can make a conjecture about how your distance from the wall is related to how much of the wall you can see in your field of vision.
3. After you feel that you understand how your initial viewing tube works, try other sizes of viewing tubes and try to see how this changes the patterns that you find. See what conjectures you can make. We'd like to be able to predict the field of vision for any viewing tube.
4. Once you are confident of your conjectures, see if you can find arguments that would convince a reasonable skeptic that your conjectures are correct.
Write up: Explain what you did, what you found, the conjectures that you made, and whatever evidence you have that they are correct. You should try to write your explanation so that it would convince one of your peers that your conclusions are correct.

Bonus Door B: Where is Your Thumb?

## Bonus Door C: Who is the Murderer?

## The Plilerklu

Thaxdey, Feturuty 19, 2009

## Police Seek Suspect



## Police Seek Suspect

Police were summoned at midnight to a grizzly murder scene at the apartment of Eddie the Weasel, a notonious criminal with underworld connections. Upon arrival, the police criminologist recorded the air temperature as a mild $68^{\circ} \mathrm{F}$ and the body temperature of the dead criminal at $85^{\circ}$ F At $2: 00$ am, after fingerprints had been taken and suspects questioned, the body had
further cooled to $74^{\circ} \mathrm{F}$.
Acting on a secure tip, the police arrested Clare Voyant, Eddie's visionary girl friend. Claxe had spent the evening in a local restaurant. Angered by being stood up once again, Clare stormed out at $11: 15$ pm , boldly threatening to kill Eddie. Although it looked like an open-and-shut case, Clare claimed she was innocent

## Bonus Door D: A Penny (or more) For Your Thoughts


pennies data collection


## Resources: Connecting with Your Mathematics Students

1) http://www.intmath.com/blog/how-to-make-math-class-interesting
2) https://www.edutopia.org/blog/engaging-students-in-math-jose-vilson

## Thanks for participating!

## Enjoy the rest of the conference!

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